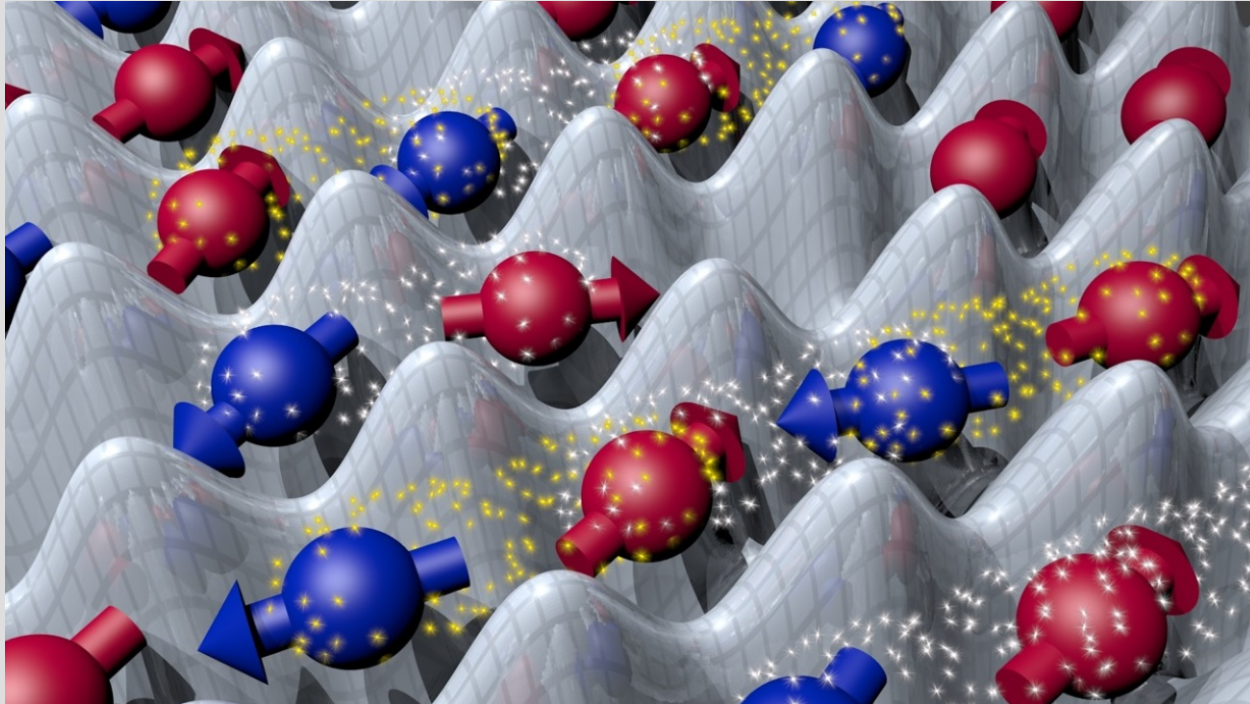
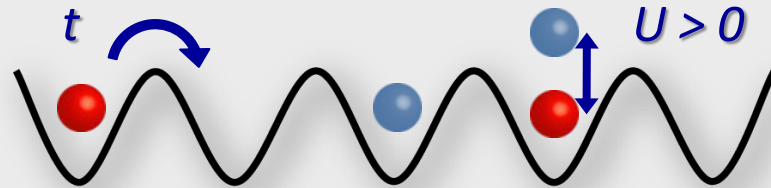
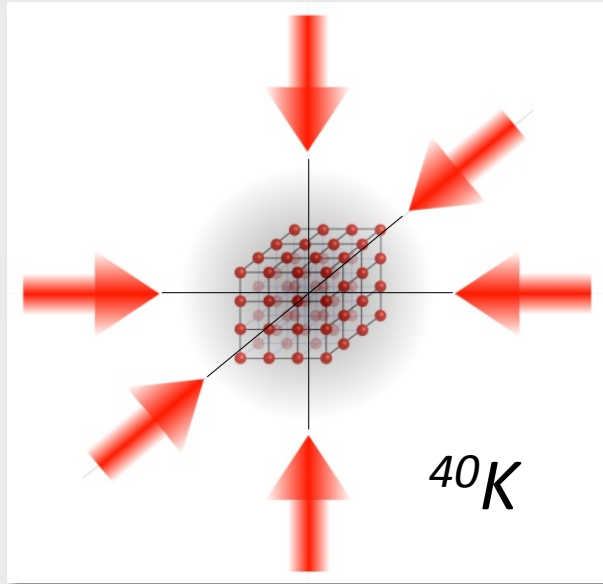


Short-range quantum magnetism of ultracold fermions in an optical lattice



Leticia Tarruell

The repulsive Fermi-Hubbard model

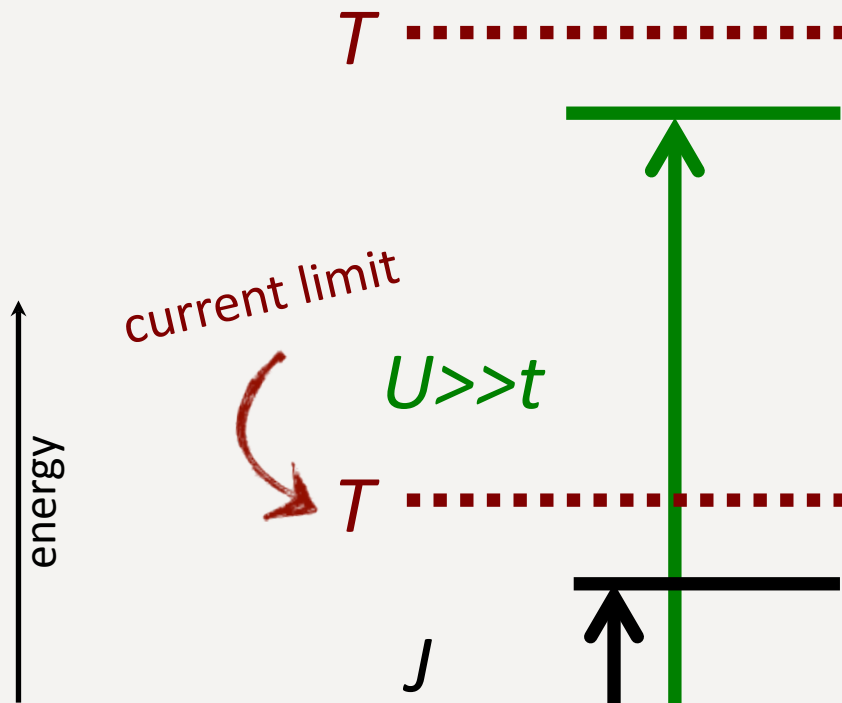


$$H_{\text{F-H}} = -t \sum_{\langle i,j \rangle, \sigma} \left(c_{i\sigma}^\dagger c_{j\sigma} + \text{h.c.} \right) + U \sum_i n_{i\uparrow} n_{i\downarrow}$$

Antiferromagnetic spin interaction from super-exchange

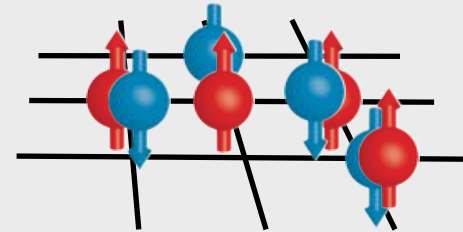
$$J = 4t^2/U$$

A temperature challenge

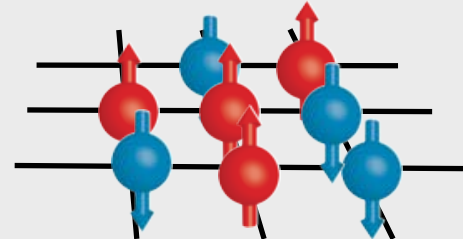


R. Jördens *et al.*, Phys. Rev. Lett. **104**, 180401 (2010)

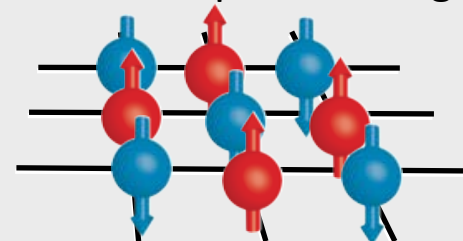
$T > U$: metallic behaviour



$T < U$: Mott insulator

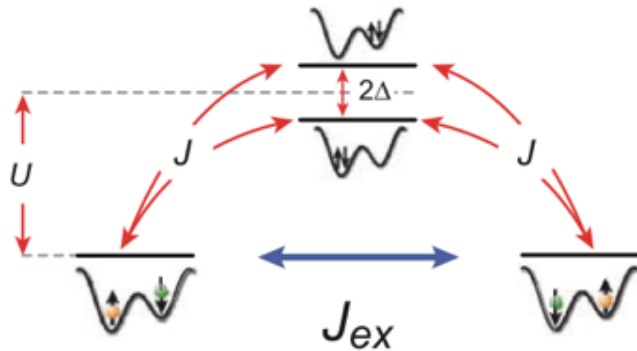


$T < J$: spin ordering



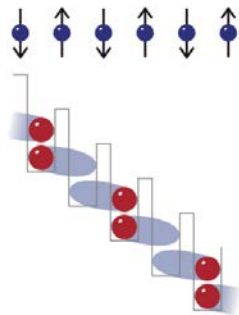
Approaches to magnetism

Isolated double-wells or plaquettes (Munich)



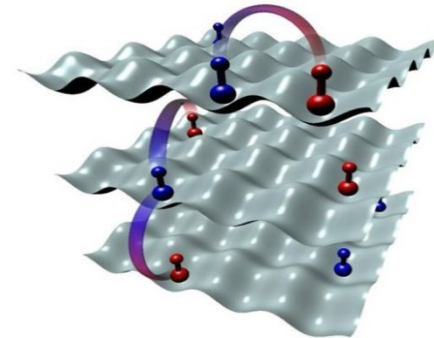
S. Trotzky *et al.*, Science **319**, 295 (2008)
S. Nascimbène *et al.*, Phys. Rev. Lett. **108**, 205301 (2012)

Mapping: Ising spin chains (Harvard)



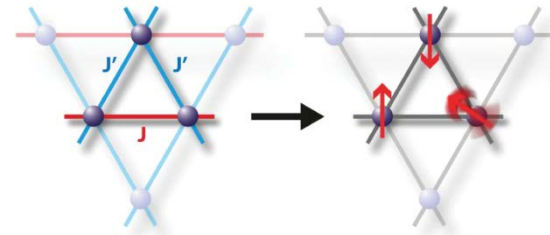
J. Simon *et al.*, Nature **472**, 307 (2011)

Dipolar interactions (JILA, Paris)



B. Yan *et al.*, Nature **501**, 521-525 (2013)
A. de Paz *et al.*, Phys. Rev. Lett. **111**, 185305 (2013)

Classical magnetism (Hamburg)



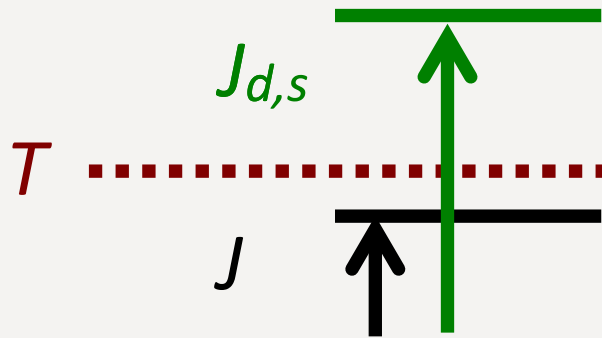
J. Struck *et al.*, Science **333**, 996 (2011)

Our approach: an energy trick

Quantum magnetism

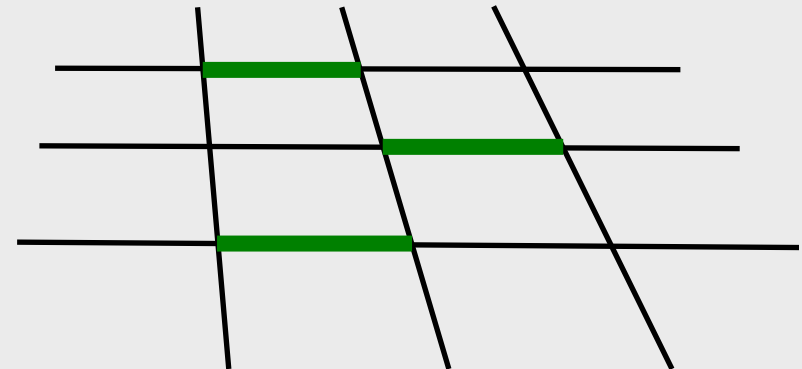
$$T < J$$

energy ↑



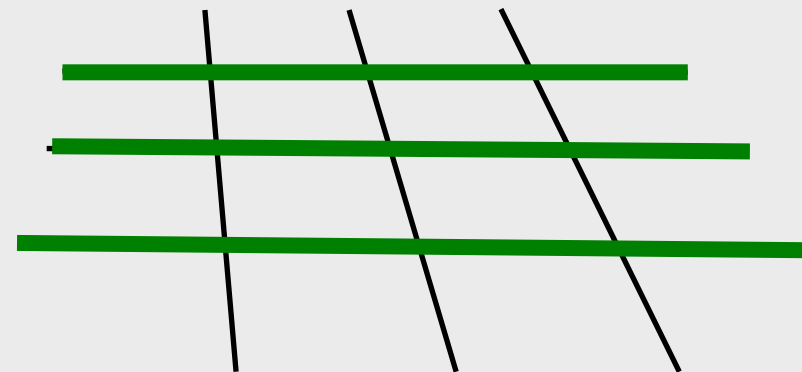
$$J < T < J_{d,s}$$

$$J_d > J$$



Dimerized lattice

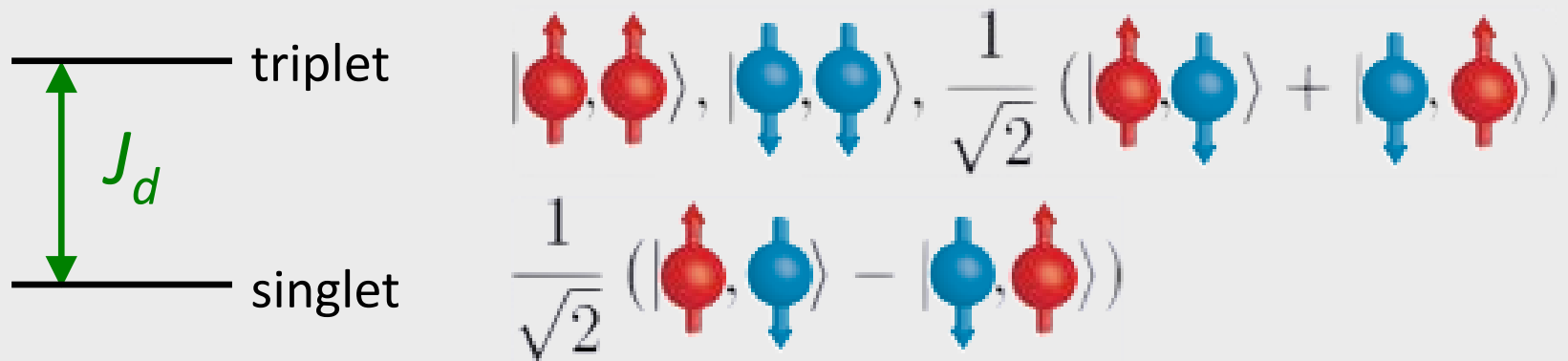
$$J_s > J$$



Anisotropic cubic lattice

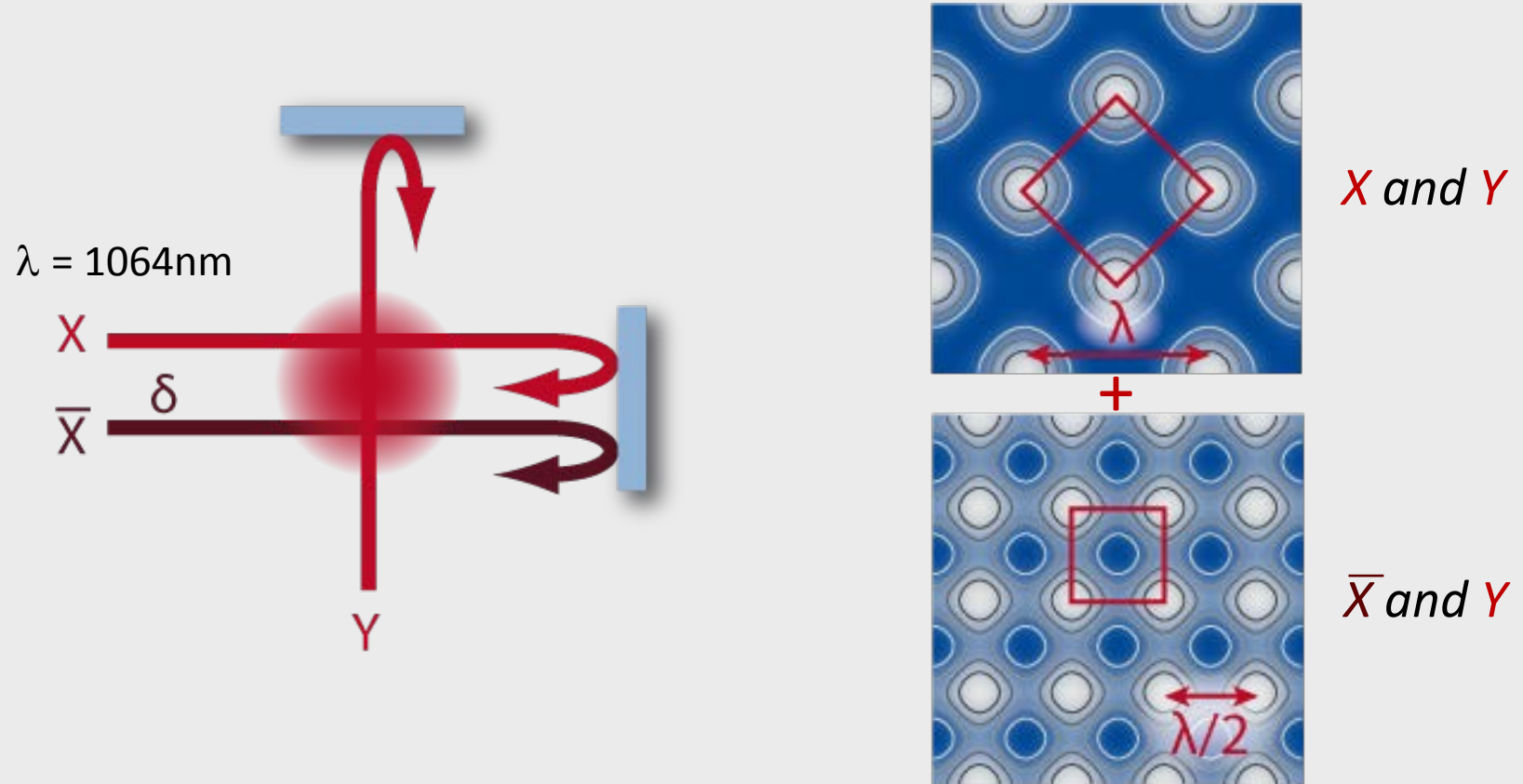
Detecting magnetic correlations

Spin correlations on neighboring sites



$$T < J_d : N_S > N_T$$

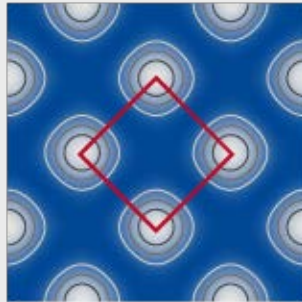
Our tool: tunable-geometry optical lattice



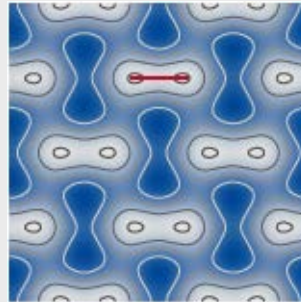
$$V(x, y) = \boxed{V_{\bar{X}} \cos^2(kx + \theta/2)} + \boxed{V_X \cos^2(kx) + V_Y \cos^2(ky) + 2\alpha\sqrt{V_X V_Y} \cos(kx) \cos(ky)}$$

Our tool: tunable-geometry optical lattice

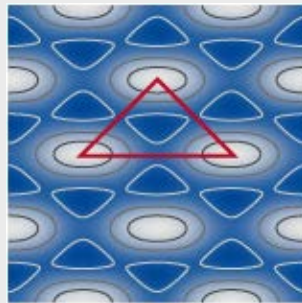
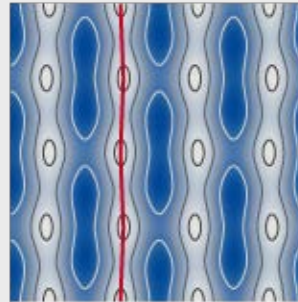
Chequerboard



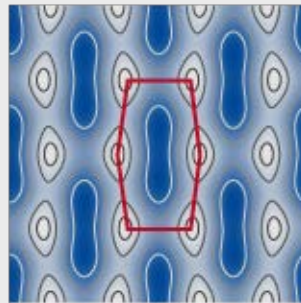
Dimer



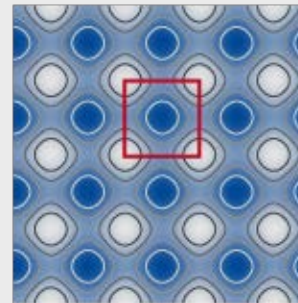
1D chains



Triangular



Honeycomb



Square

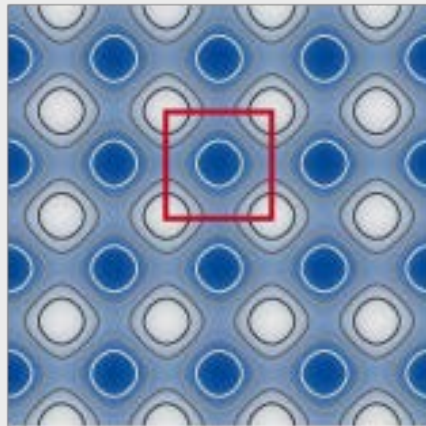
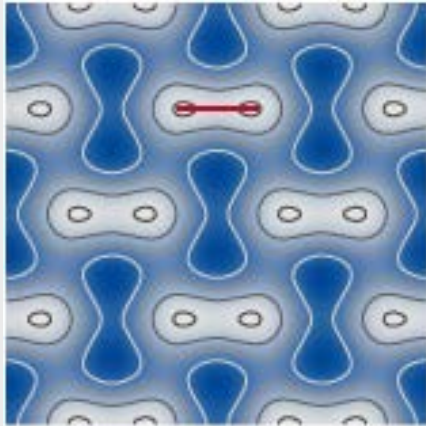


L. Tarruell *et al.*,
Nature **483**, 302 (2012)

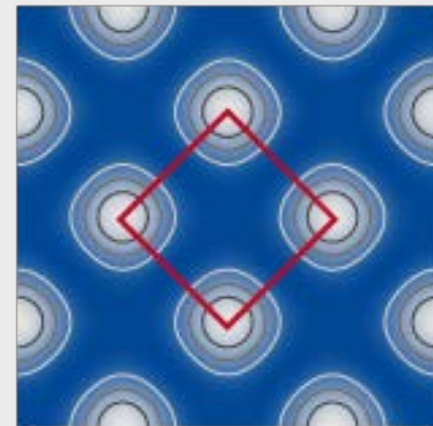
Other non-standard lattices: NIST, Munich, Bonn, Hamburg, Berkeley

Merging lattice sites

Dimer

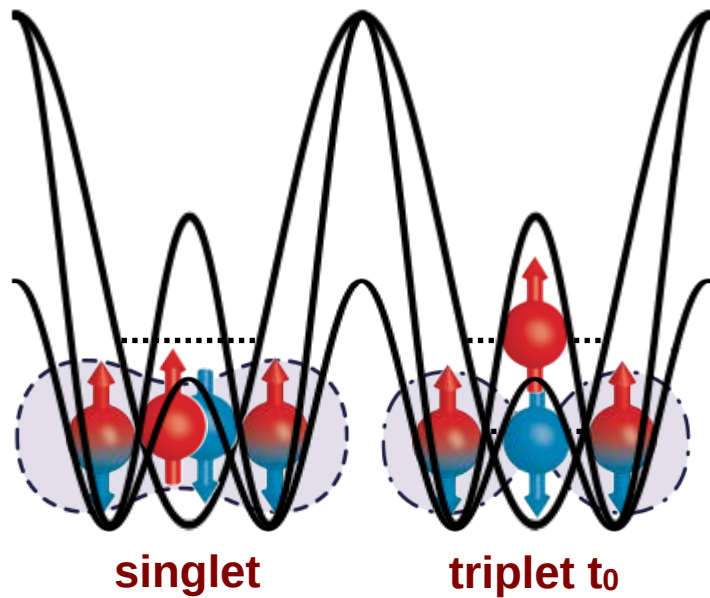


Square

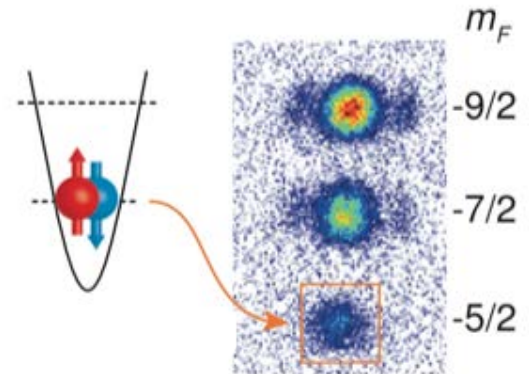


Chequerboard

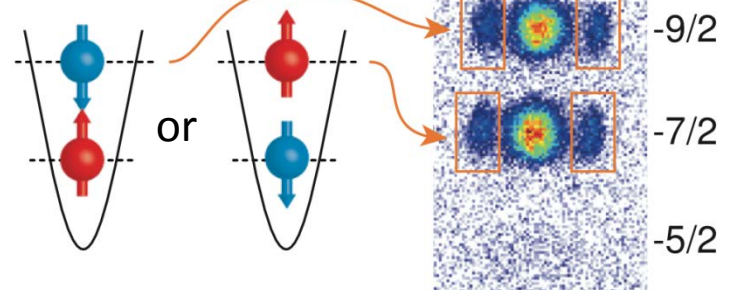
Detecting magnetic correlations



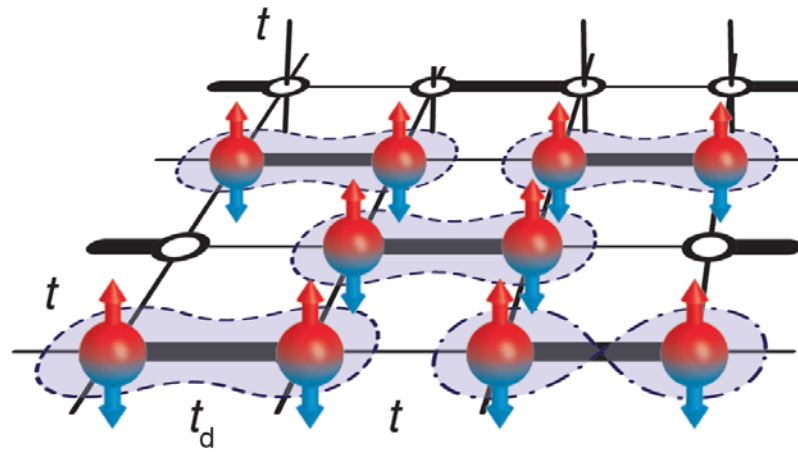
singlet



triplet t_0



Dimerized lattice

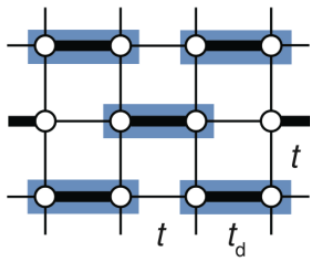


Dimerized cubic lattice

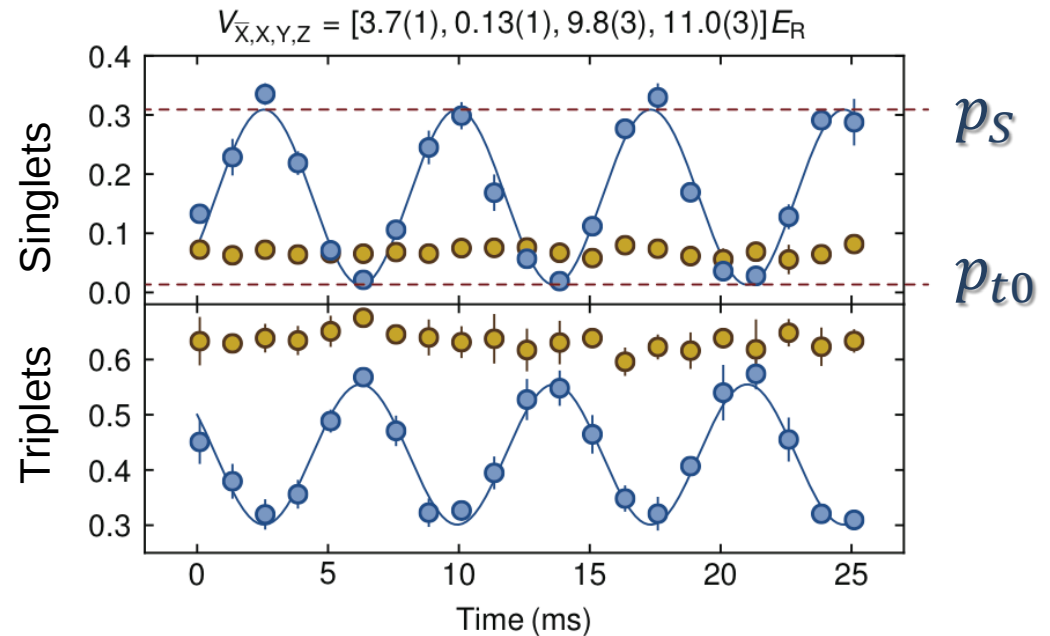


Measuring singlets and triplets

Merging neighboring sites



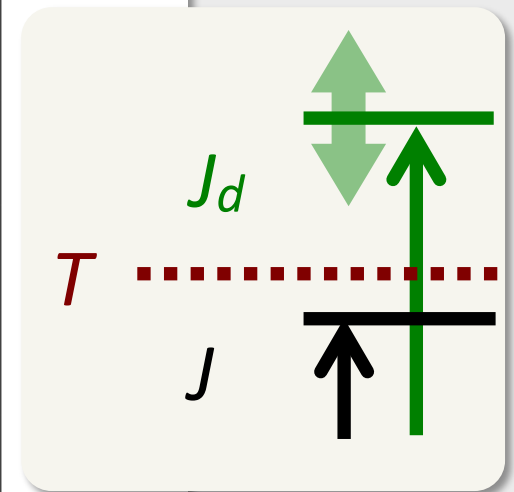
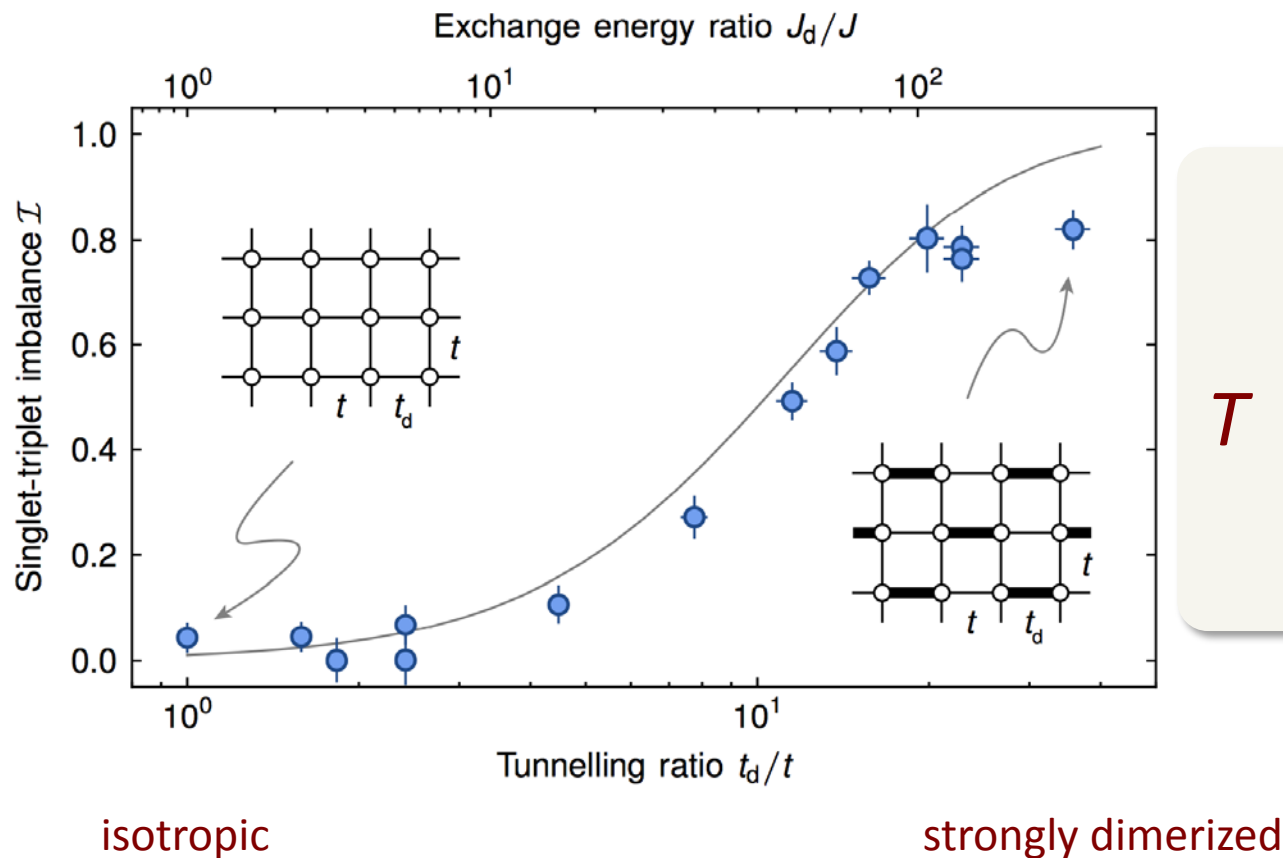
Singlet-triplet oscillations



Singlet-Triplet Imbalance
$$\mathcal{I} = \frac{p_s - p_{t0}}{p_s + p_{t0}}$$

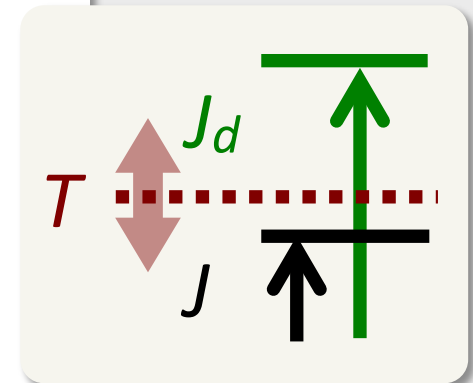
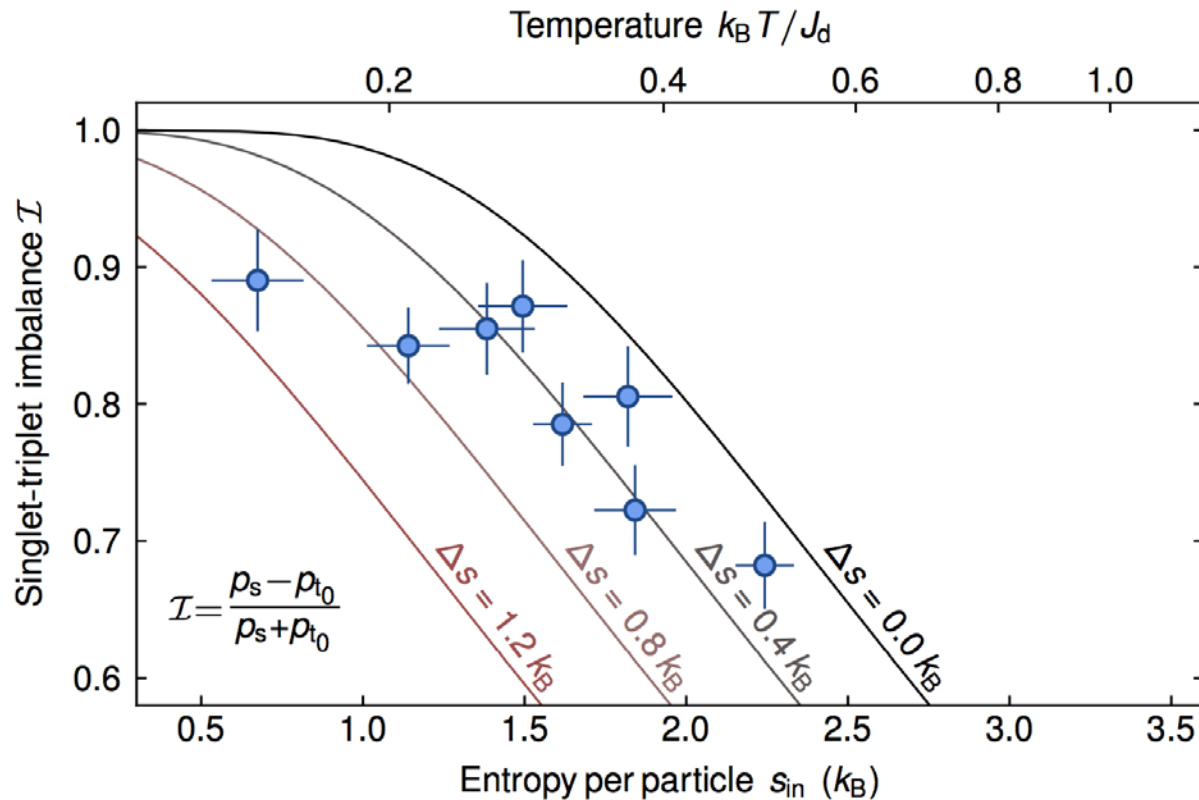
Singlet-triplet oscillations: S. Trotzky *et al.*, Phys. Rev. Lett. **105**, 265303 (2010)

Dependence on dimerization



Theory: second order high-temperature series expansion of coupled dimers $s=1.7 k_B$

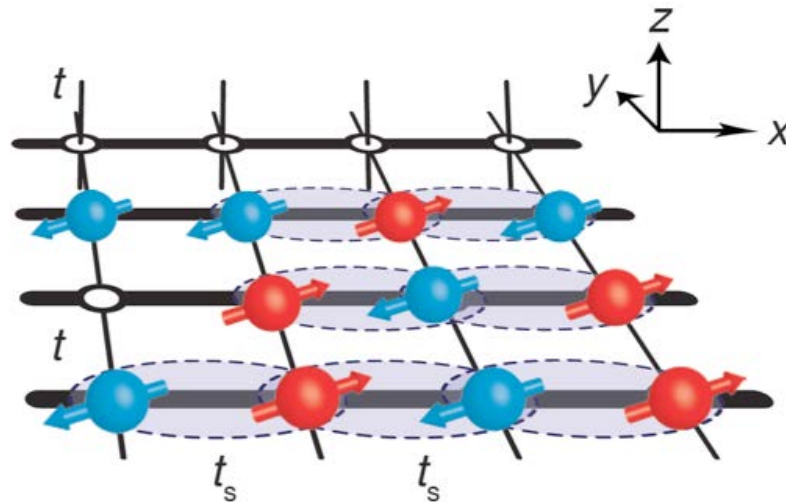
Dependence on entropy



Theory: second order high-temperature series expansion of coupled dimers

$U/t = 11.0(8)$
 $t_d/t = 22(2)$
 $t/h = 67(3) \text{ Hz}$

Anisotropic cubic lattice



Effective 1D chains

AFM correlations along x

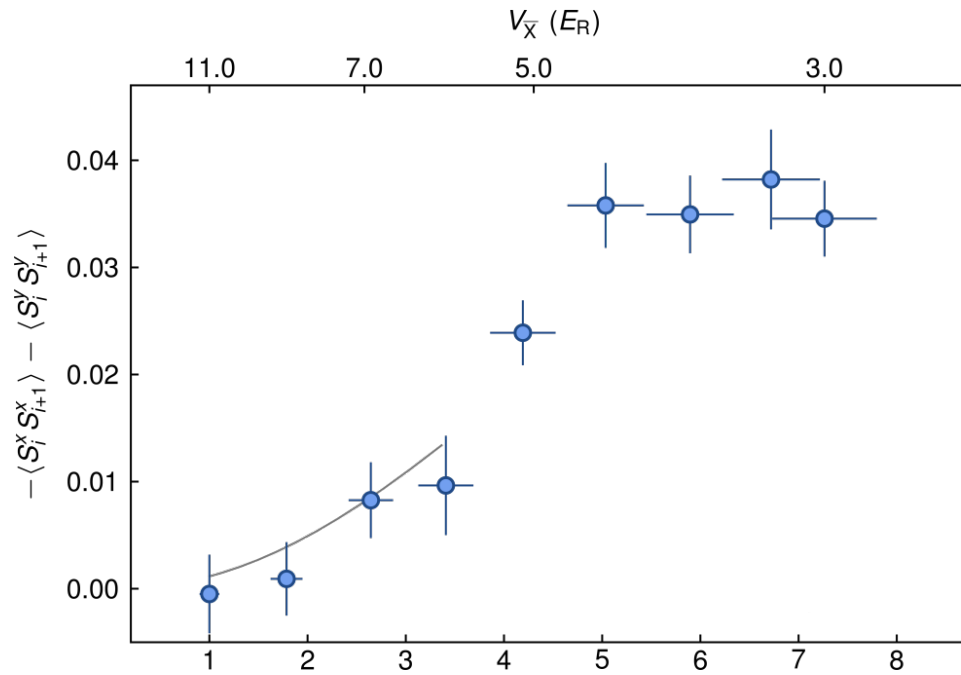
$$\langle \mathbf{S}_i \cdot \mathbf{S}_{i+1} \rangle \neq 0$$

transverse spin correlator $\Leftrightarrow$ population difference

$$- \langle S_i^x S_{i+1}^x \rangle - \langle S_i^y S_{i+1}^y \rangle = (p_s - p_{t_0}) / 2$$

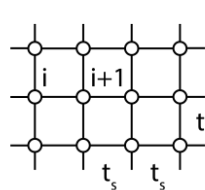
Redistribution of entropy: incoherent spin chains, entropy stored in between

Dependence on anisotropy



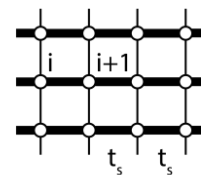
normalized spin correlator

$$\mathcal{S} = \frac{-4\langle S_i^z S_{i+1}^z \rangle}{\langle n_i^s n_{i+1}^s \rangle} = \frac{p_s - p_{t_0}}{p_s + 3p_{t_0}}$$



isotropic

Tunnelling ratio t_s/t

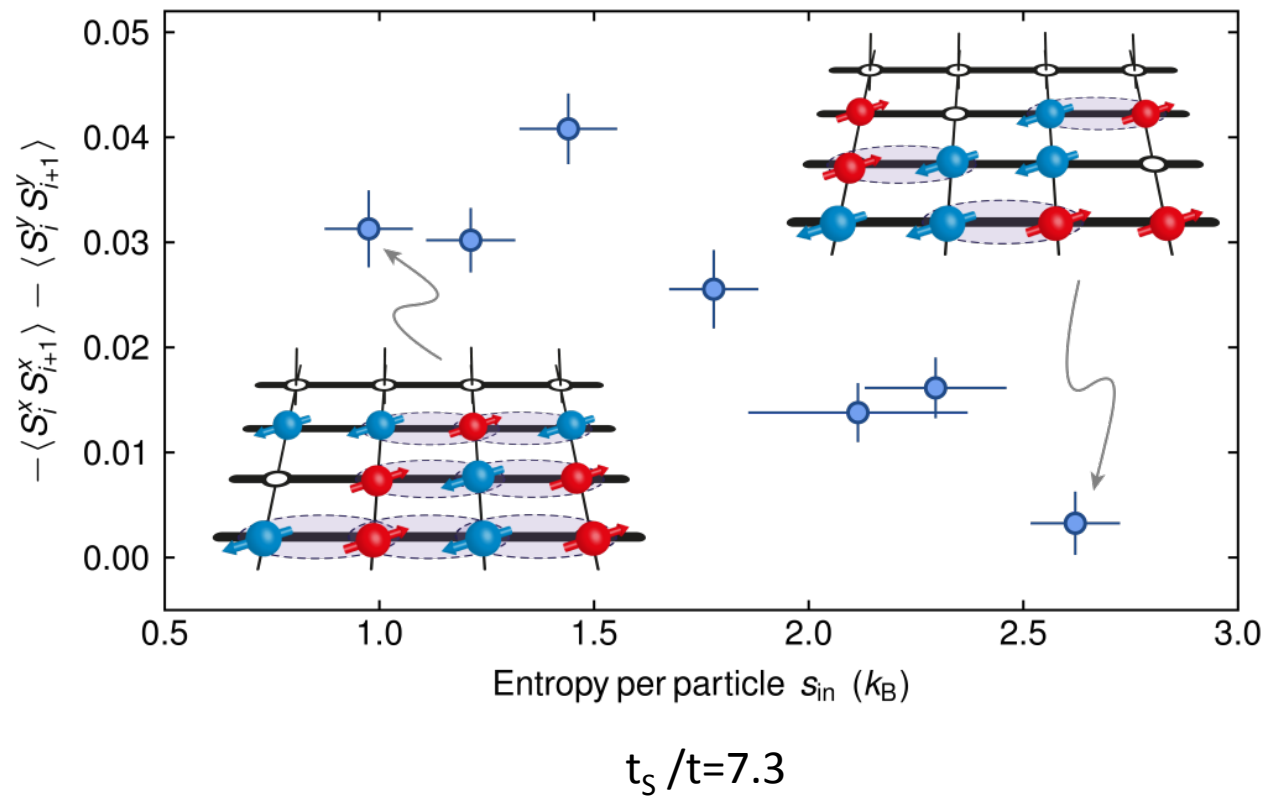


strongly anisotropic

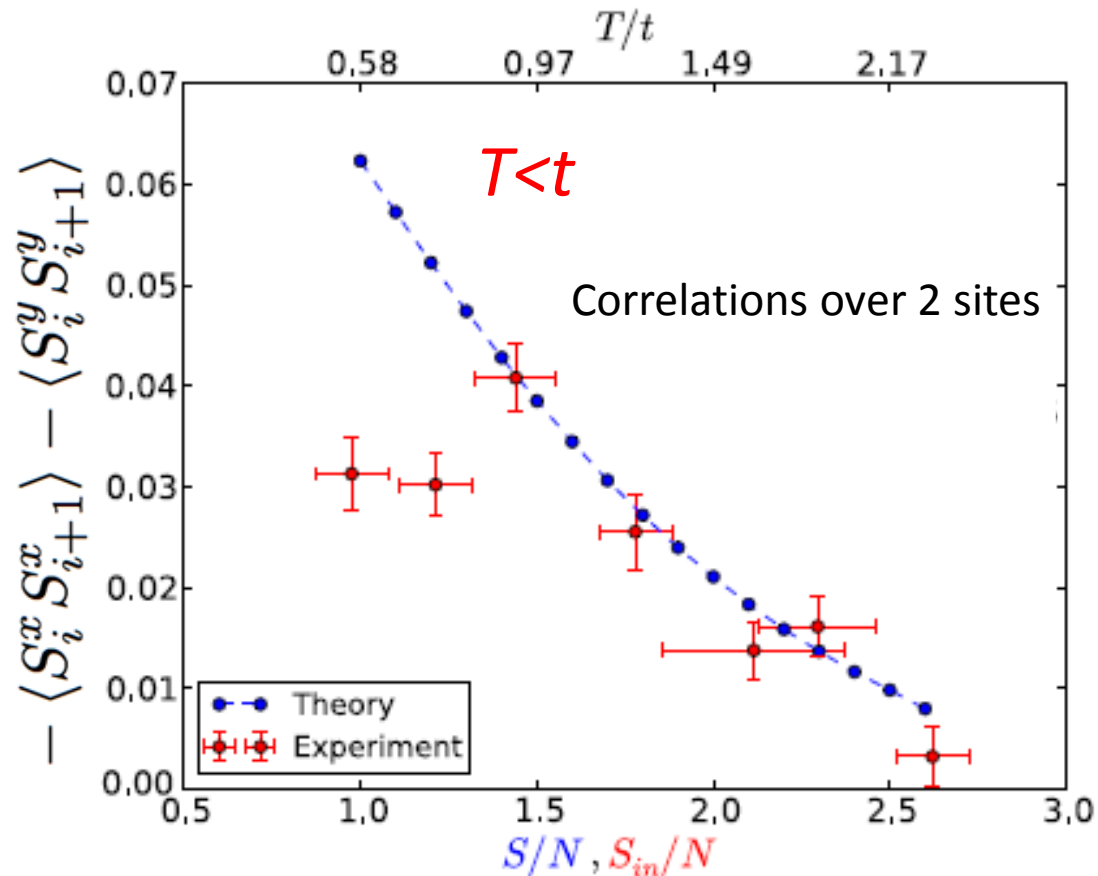
$$V_{Y,Z} = 11.0(3) E_R$$

$$s = 1.8 k_B$$

Dependence on entropy

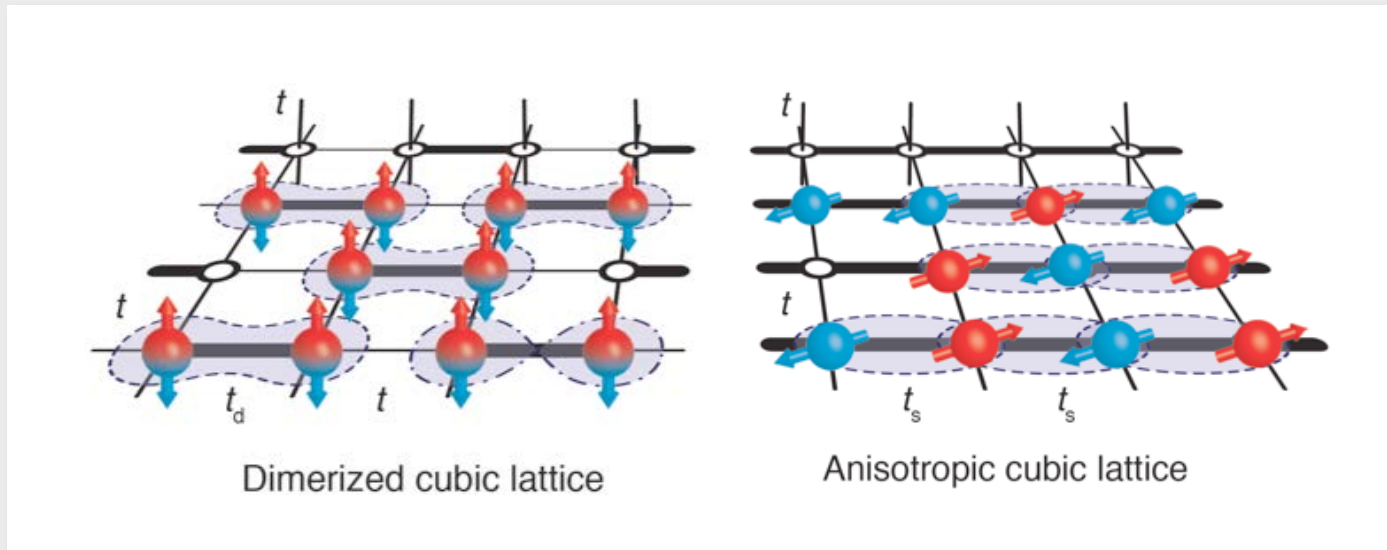


Comparison with theory



Theory: DCA+LDA for anisotropic simple cubic lattice
 J. Imriška, M. Iazzi, L. Wang, E. Gull and M. Troyer – ETH Zurich

Short-range quantum magnetism



Nearest-neighbor magnetic correlations in thermalized ensembles

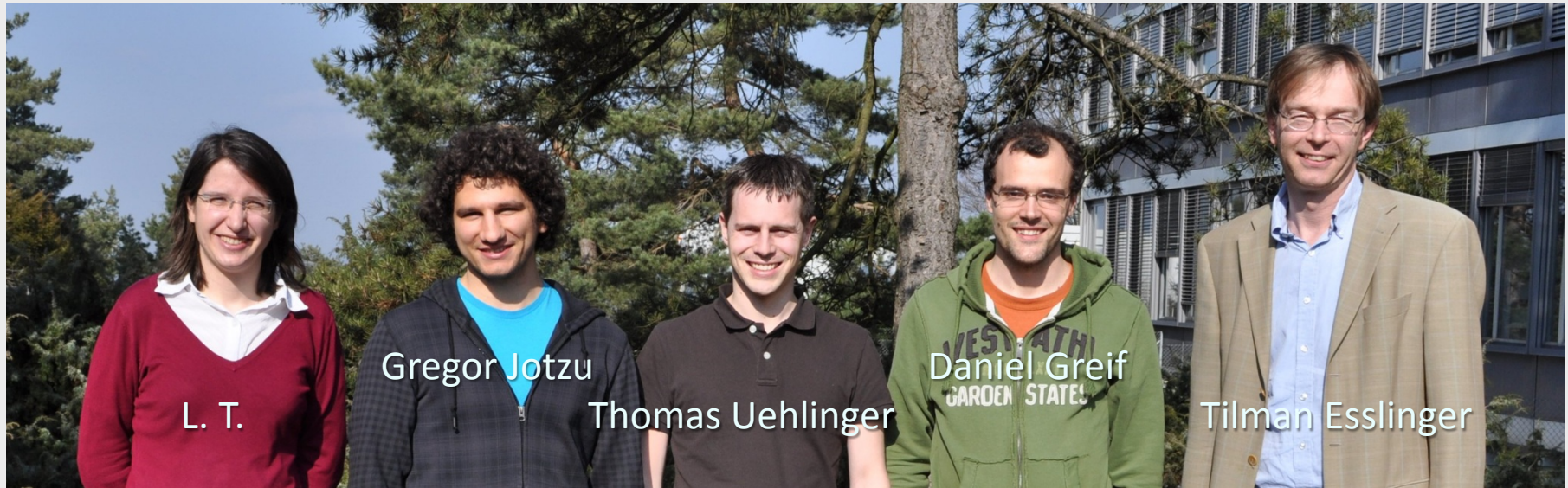
D. Greif, T. Uehlinger, G. Jotzu, L. Tarruell, and T. Esslinger, *Science* **340**, 1307 (2013)

Comparison with numerical simulations: $T < t$ in effective 1D systems

J. Imriška, M. Iazzi, L. Wang, E. Gull, D. Greif, T. Uehlinger, G. Jotzu, L. Tarruell, T. Esslinger, and M. Troyer, *Phys. Rev. Lett.* **112**, 115301 (2014)

B. Sciolle, A. Tokuno, S. Uchino, P. Bartmettler, T. Giamarchi, and C. Kollath, *Phys. Rev. A* **88**, 063629 (2013)

The ETH lattice team' 2012

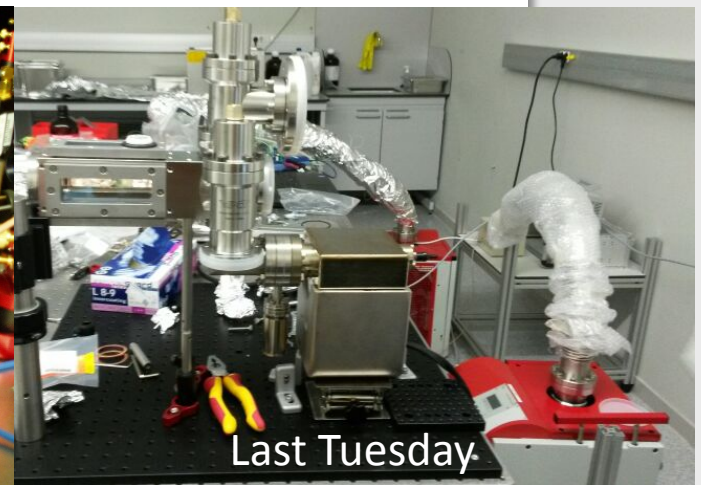
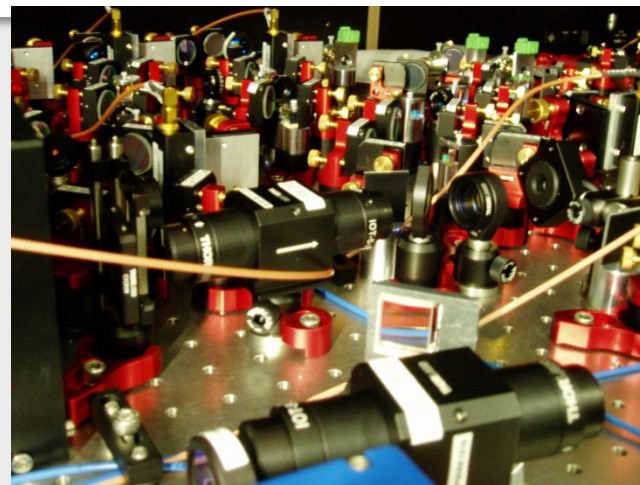
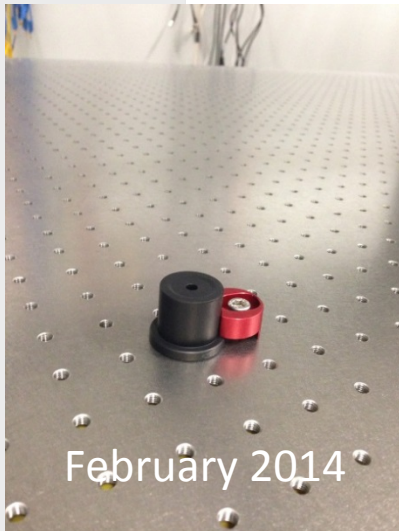
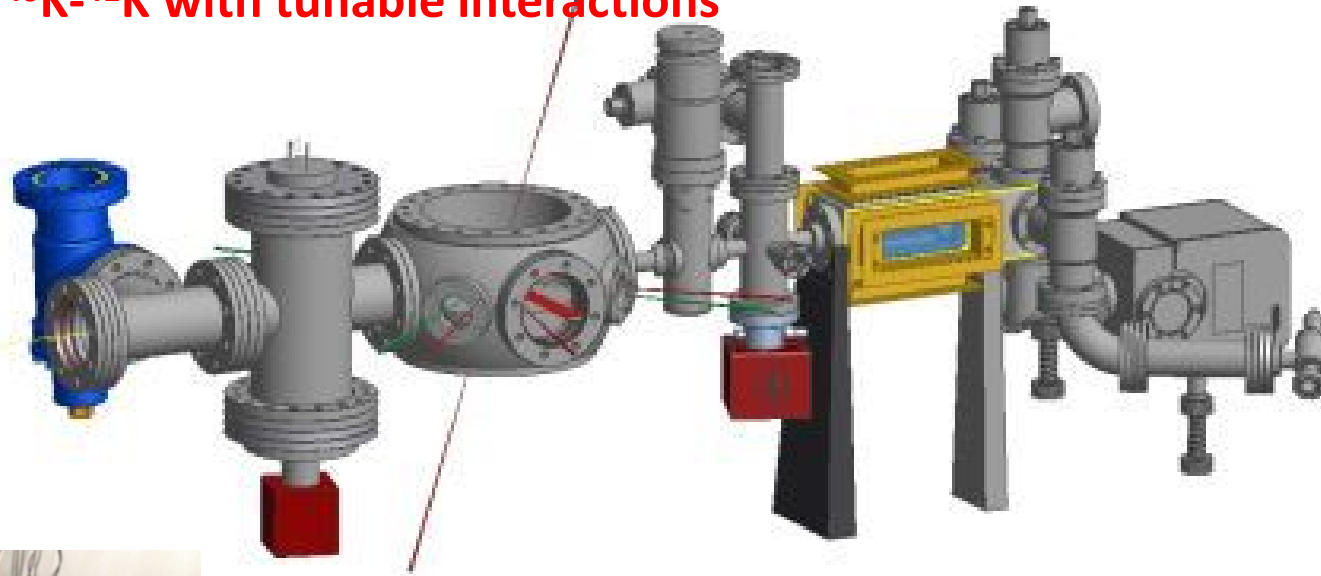


Theory: J. Imriška, M. Iazzi, L. Wang, E. Gull and M. Troyer
Many discussions with C. Kollath and T. Giamarchi's groups

Funding: EU (ERC SQMS), SNF, NCCR QSIT, NCCR MaNEP

Towards isotopic potassium mixtures

^{40}K - ^{41}K with tunable interactions



The ICFO quantum gases group' 2014



ICFO^R



**Fundació Privada
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