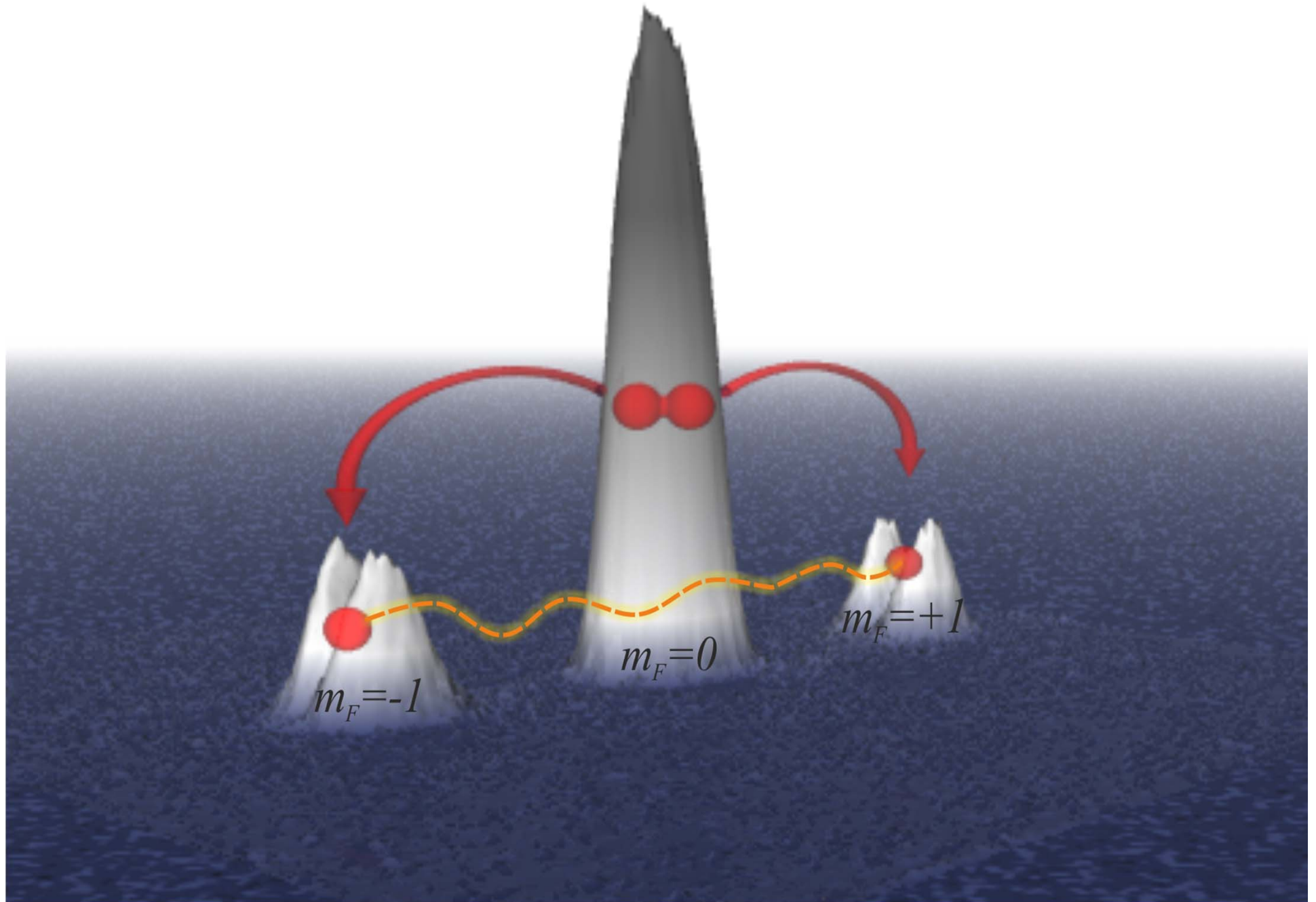
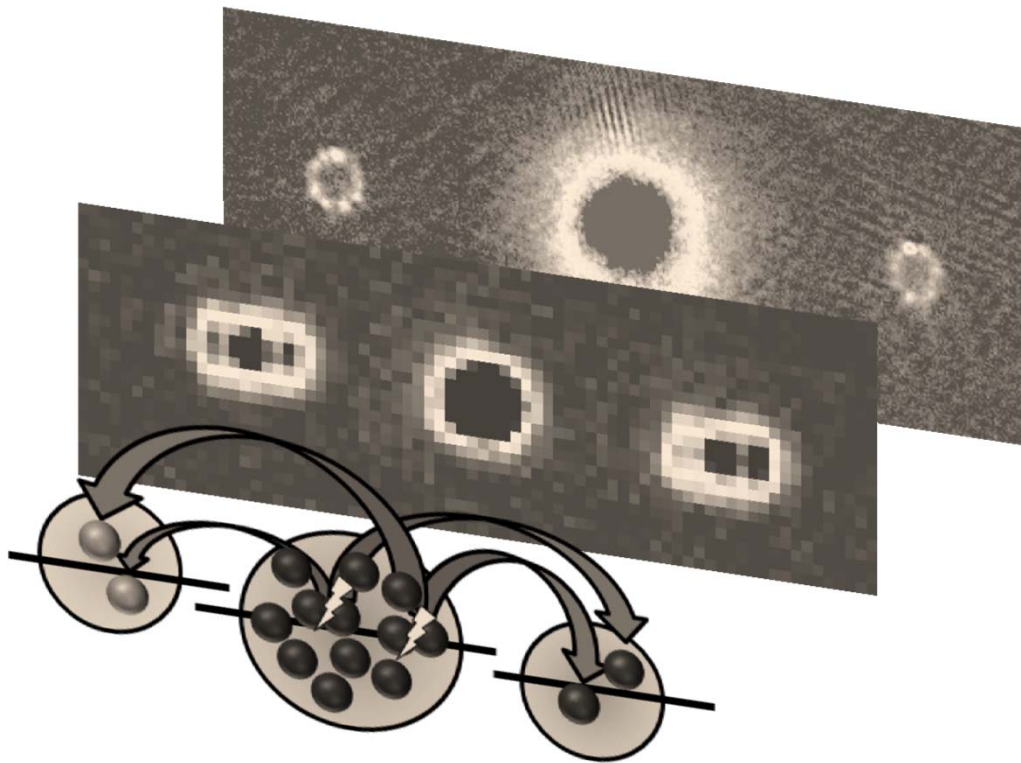


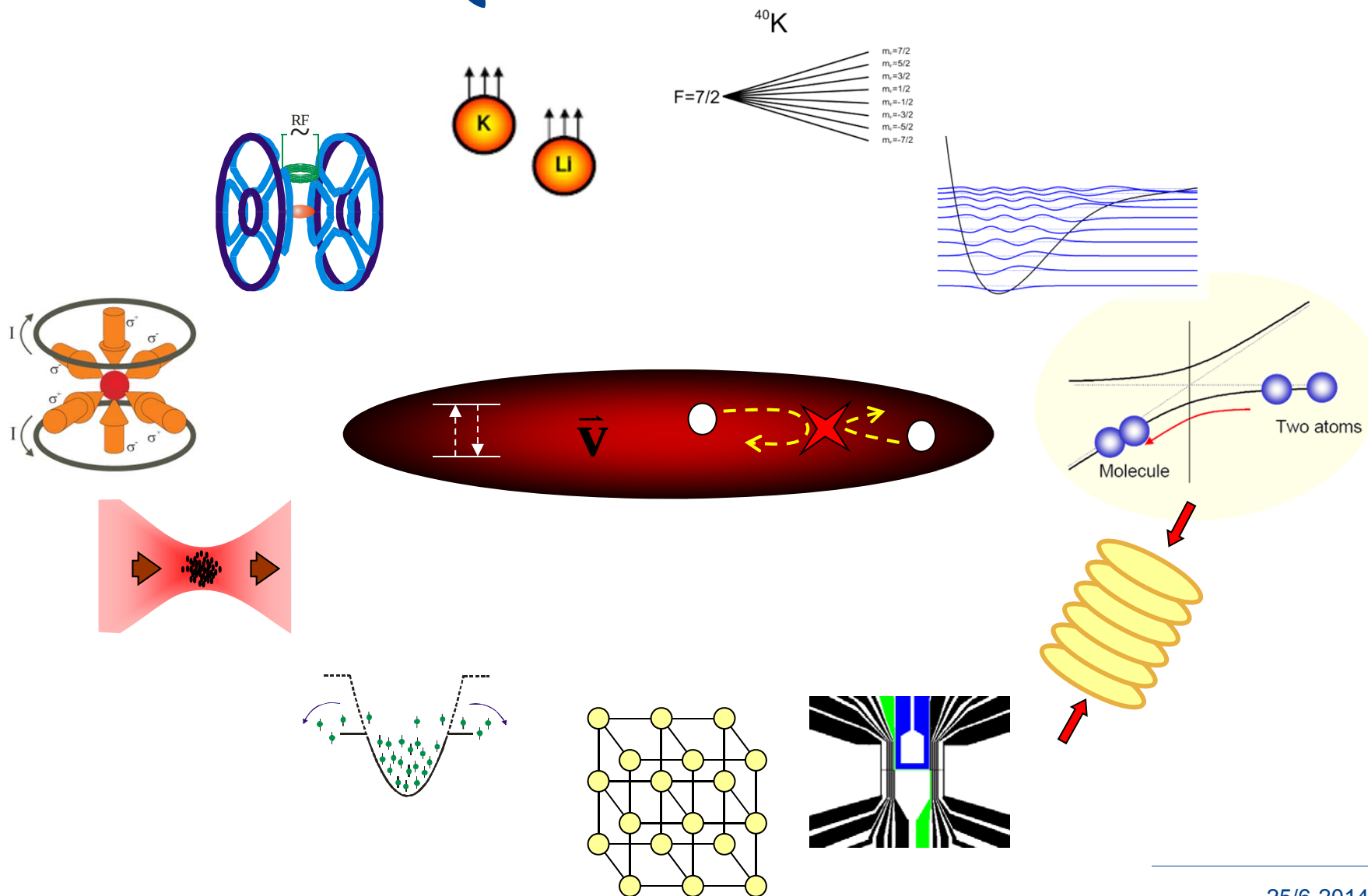


Correlations and entanglement in spinor quantum gasses

J. Arlt

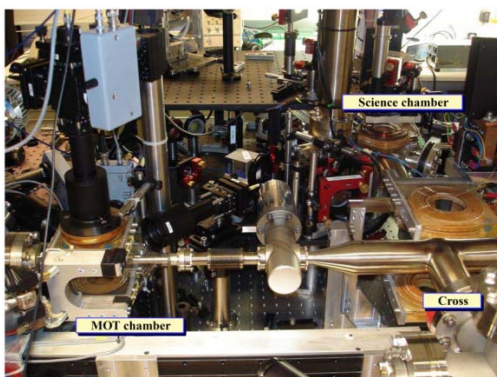


ULTRACOLD QUANTUM GASES GROUP



Experiments:

Ultracold Bosons in Optical Lattices



- Quantum optics with matter waves
- Spinor dynamics in 2D
- Faraday detection



Andrew
Hilliard

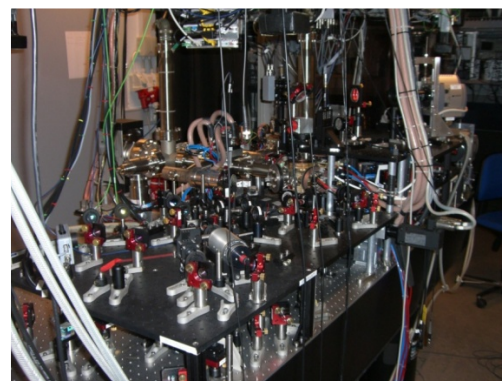


Poul
Pedersen



Miroslav
Gajdacz

Multi Species Quantum Gases



- multi-species quantum gases
- phases in tuneable mixtures
- bosonic polaron physics



Nils
Winter

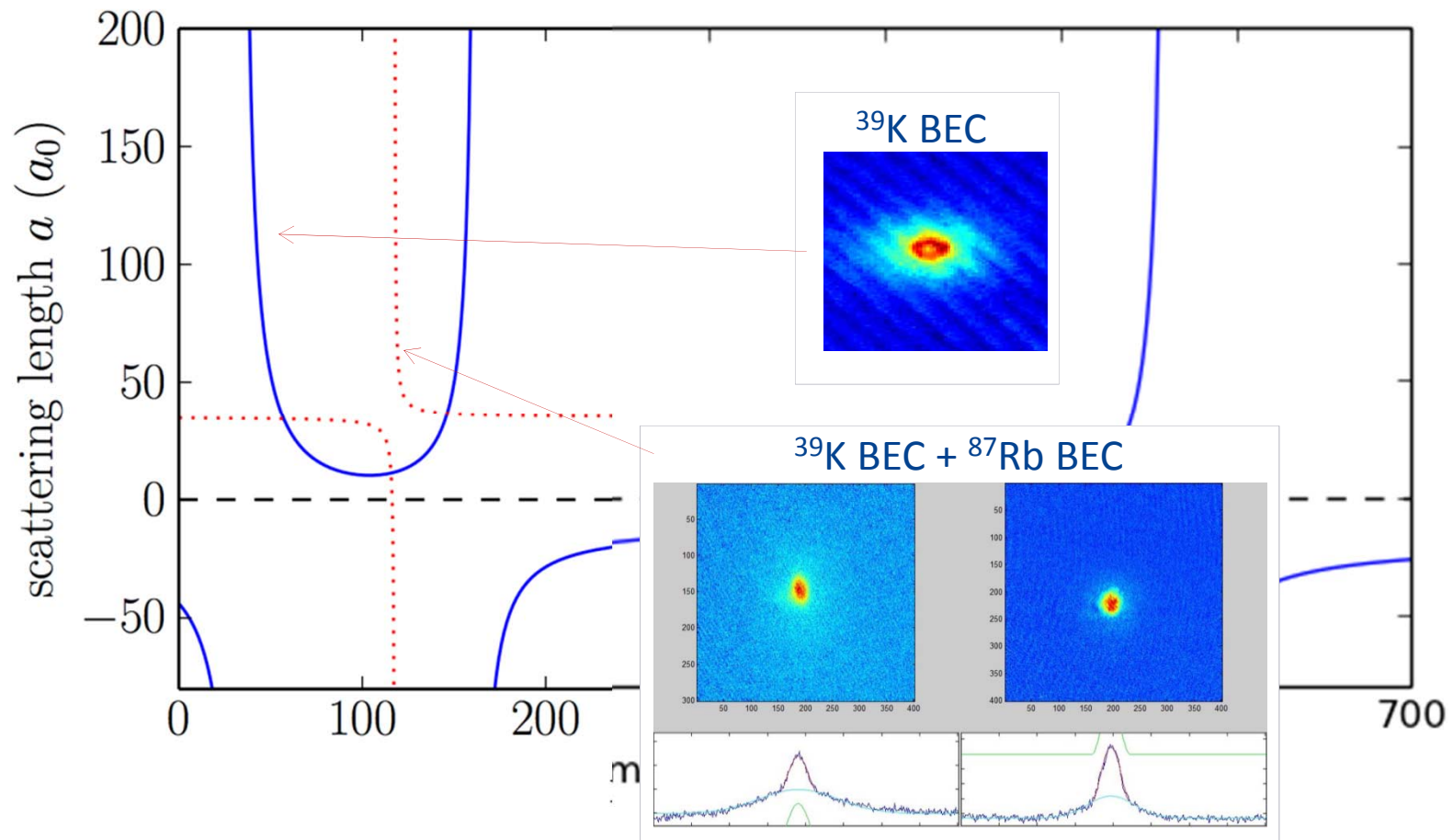


Lars
Wacker



Nils
Jørgensen

Mix - Multi Species Quantum Gases

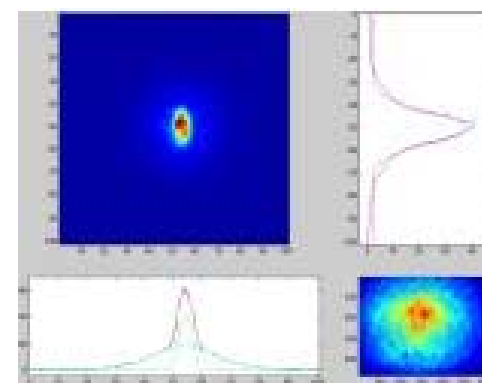
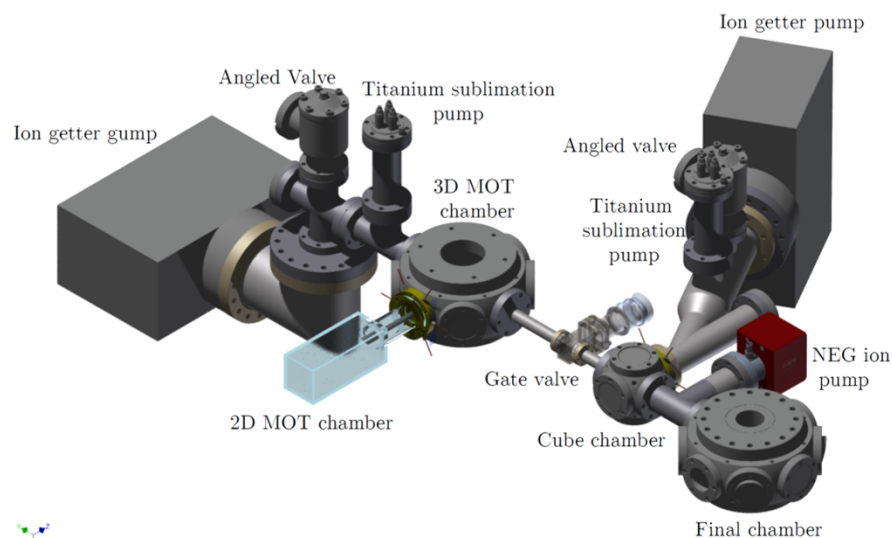


Potassium in $|F=1, m_F=-1\rangle$

HiRes - High Resolution Experiment



Jacob Sherson



Romain
Mueller



Robert
Heck

PostDocs: Mark Bason,
Wenzhuo Zhang,
Mario Napolitano



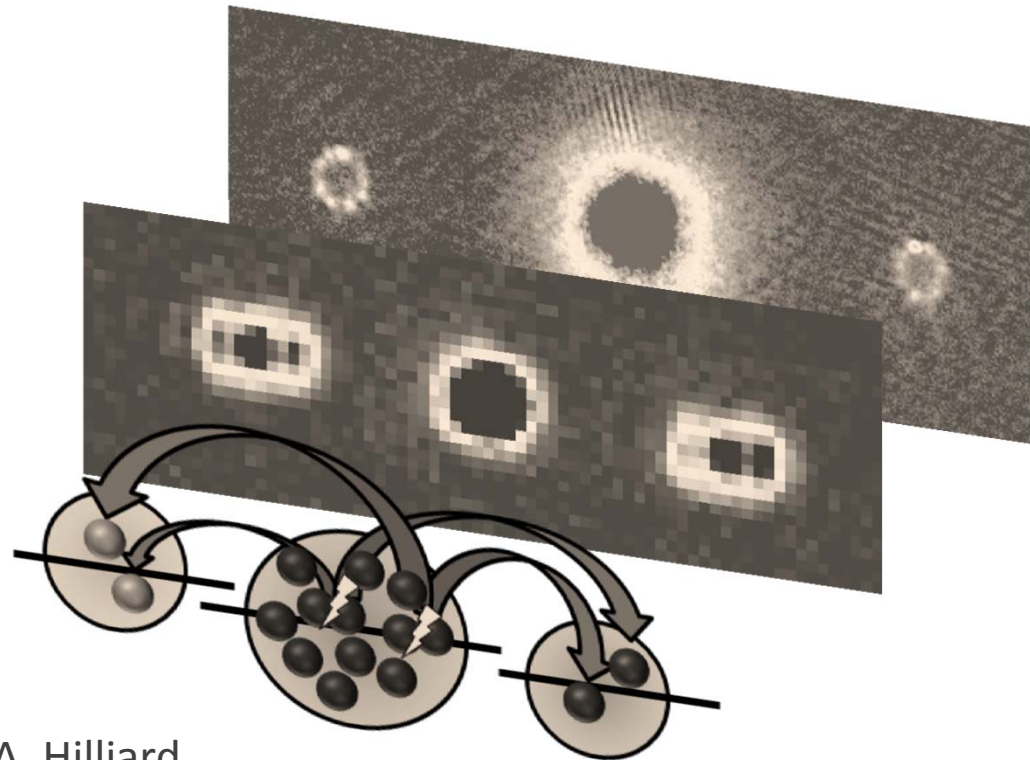
Laboratory visits:

Thursday (tomorrow) at 13:00 !

We will leave together from AIAS.
The labs are within walking
distance.

Correlations and entanglement in spinor quantum gasses

J. Arlt



P. Pedersen, M. Gajdacz, J. Sherson, A. Hilliard

Aarhus Universitet

B. Lücke, J. Peise, F. Deuretzbacher, W. Ertmer, L. Santos, C. Klempt

Leibniz Universität Hannover

G. Vitagliano, G. Tóth

University of the Basque Country

Precision Measurements in Physics

Length



...



Gravitational Wave Detector

Time

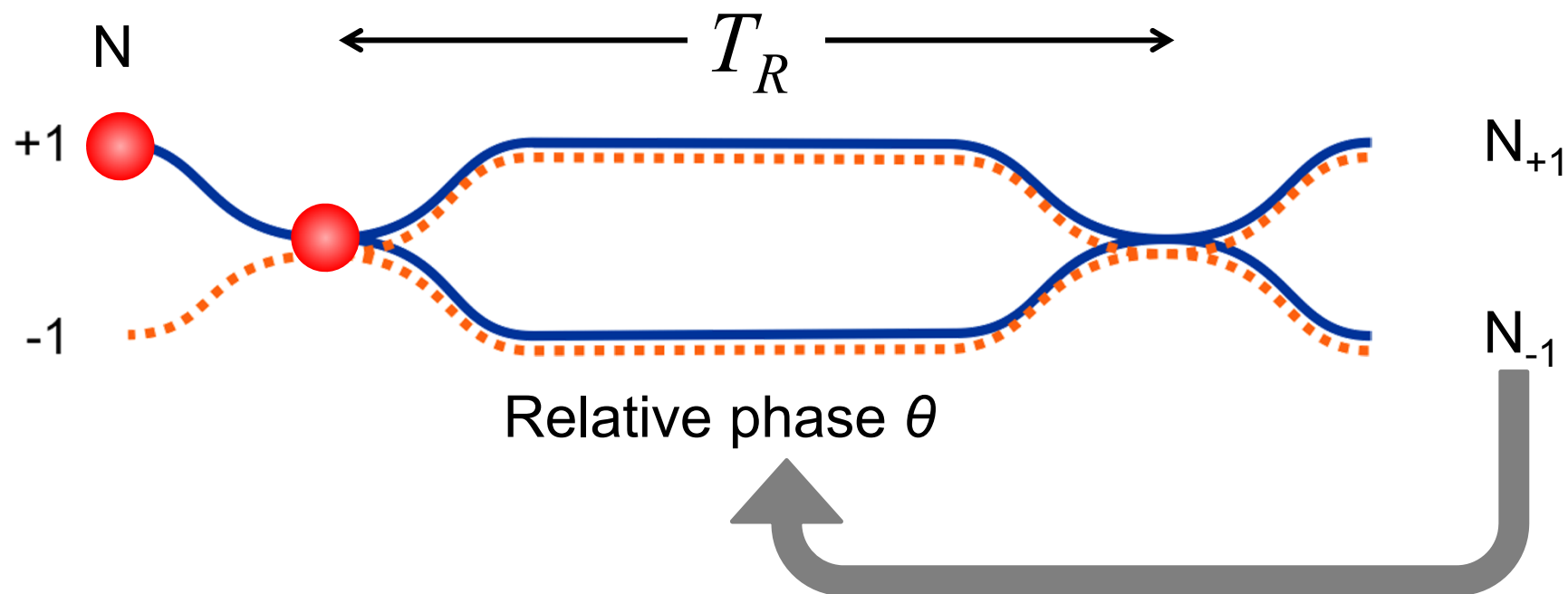


...



Atomic Clock

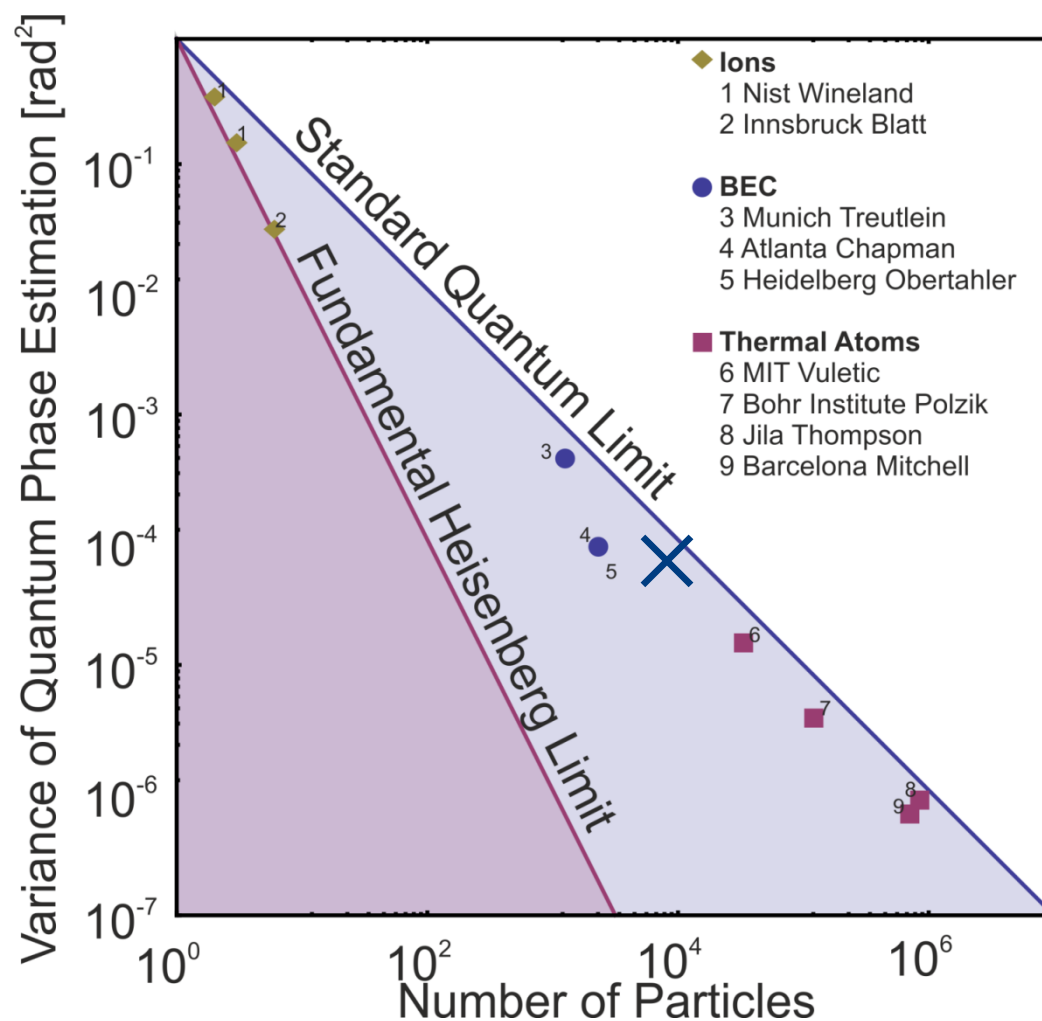
Atom interferometry



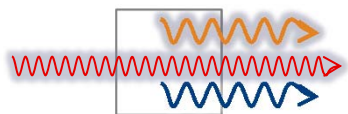
Phase estimation uncertainty:

$$\frac{\Delta\theta}{\theta}(\tau) = \frac{1}{\omega_0 T_R \sqrt{N}} \sqrt{\frac{T_{\text{prep}} + T_R}{\tau}}$$

Solution: Sub-shot-noise Interferometry



Content



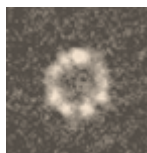
Introduction



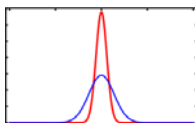
Creation of correlated states



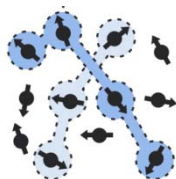
External mode control



2D correlated spinor gasses

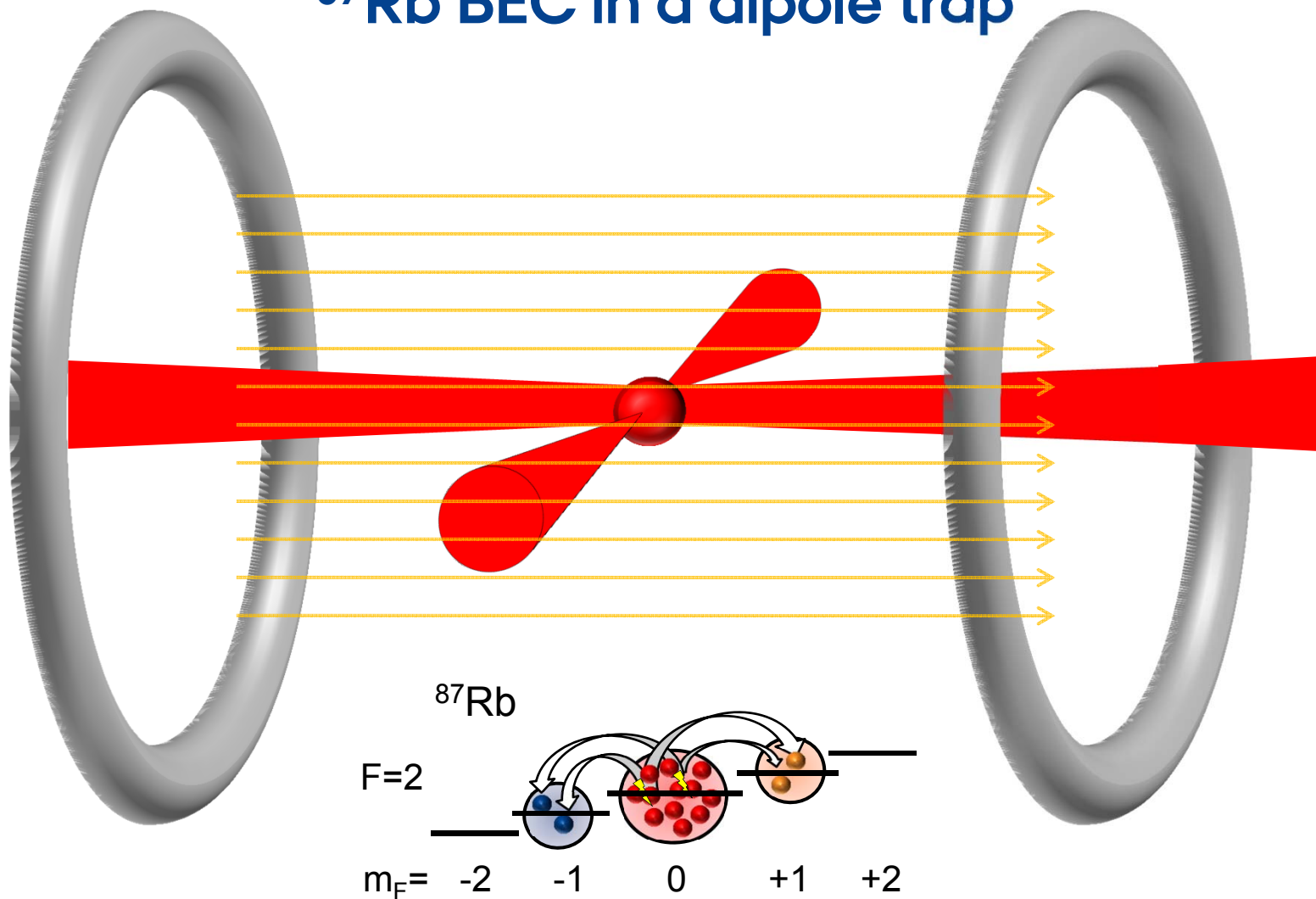


Dicke states for interferometry

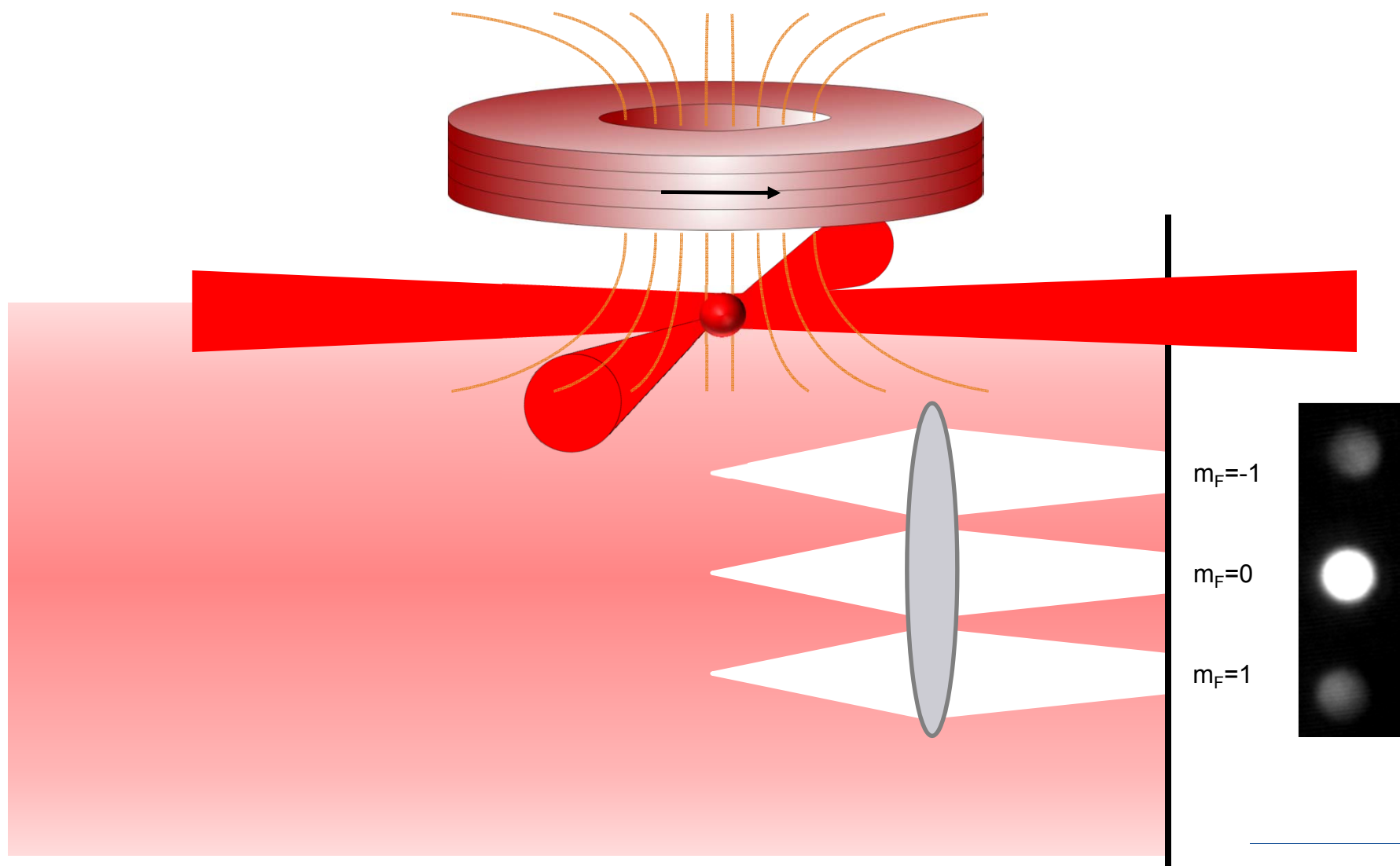


Multi-particle entanglement

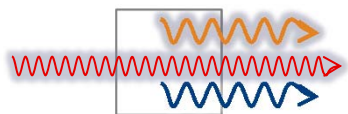
^{87}Rb BEC in a dipole trap



Absorption detection



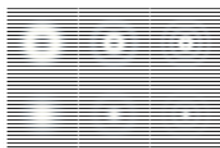
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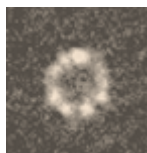
Introduction



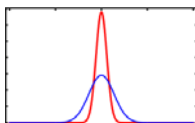
Creation of correlated states



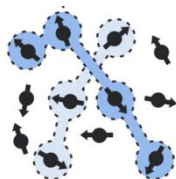
External mode control



2D correlated spinor gasses



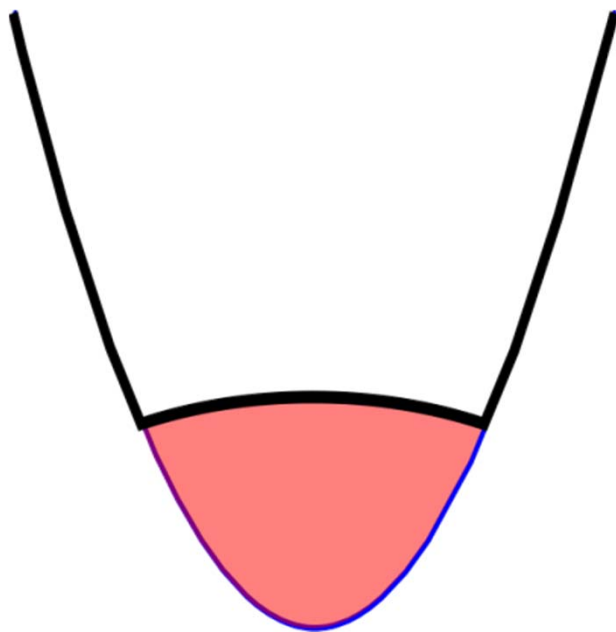
Dicke states for interferometry



Multi-particle entanglement

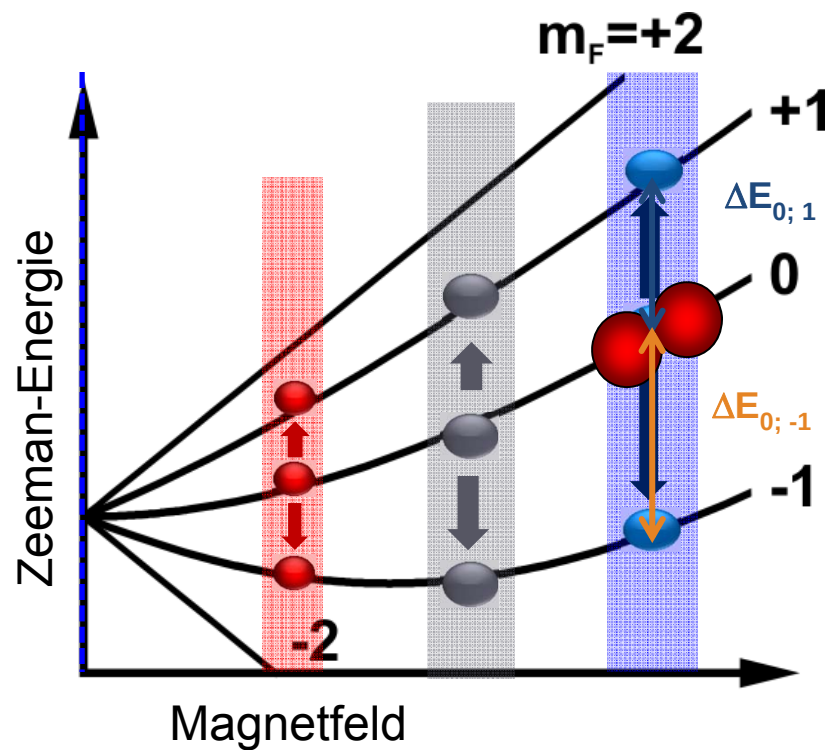
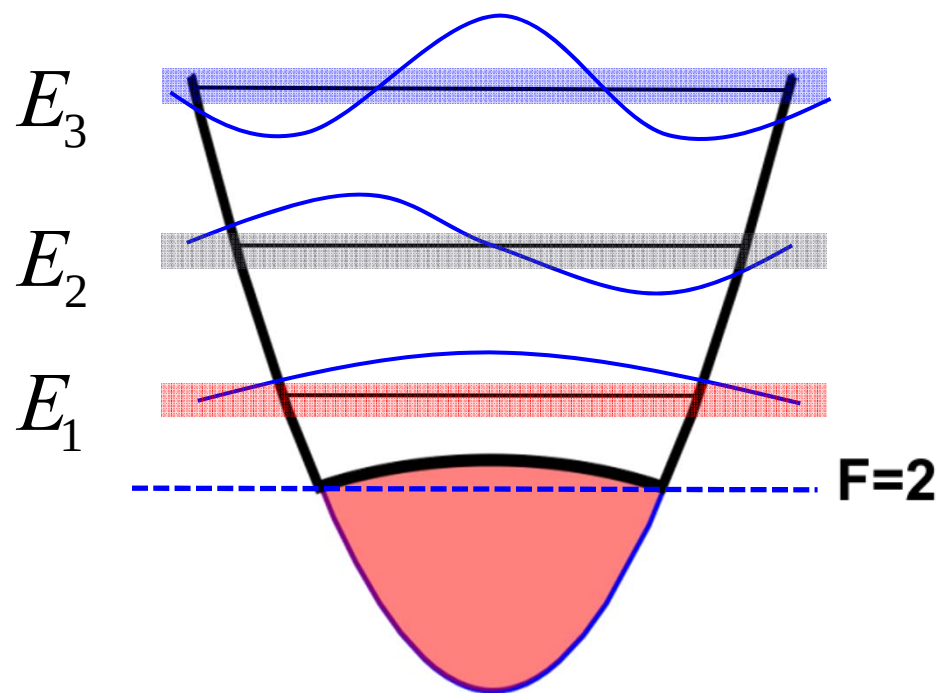
Simplified model for spin dynamics

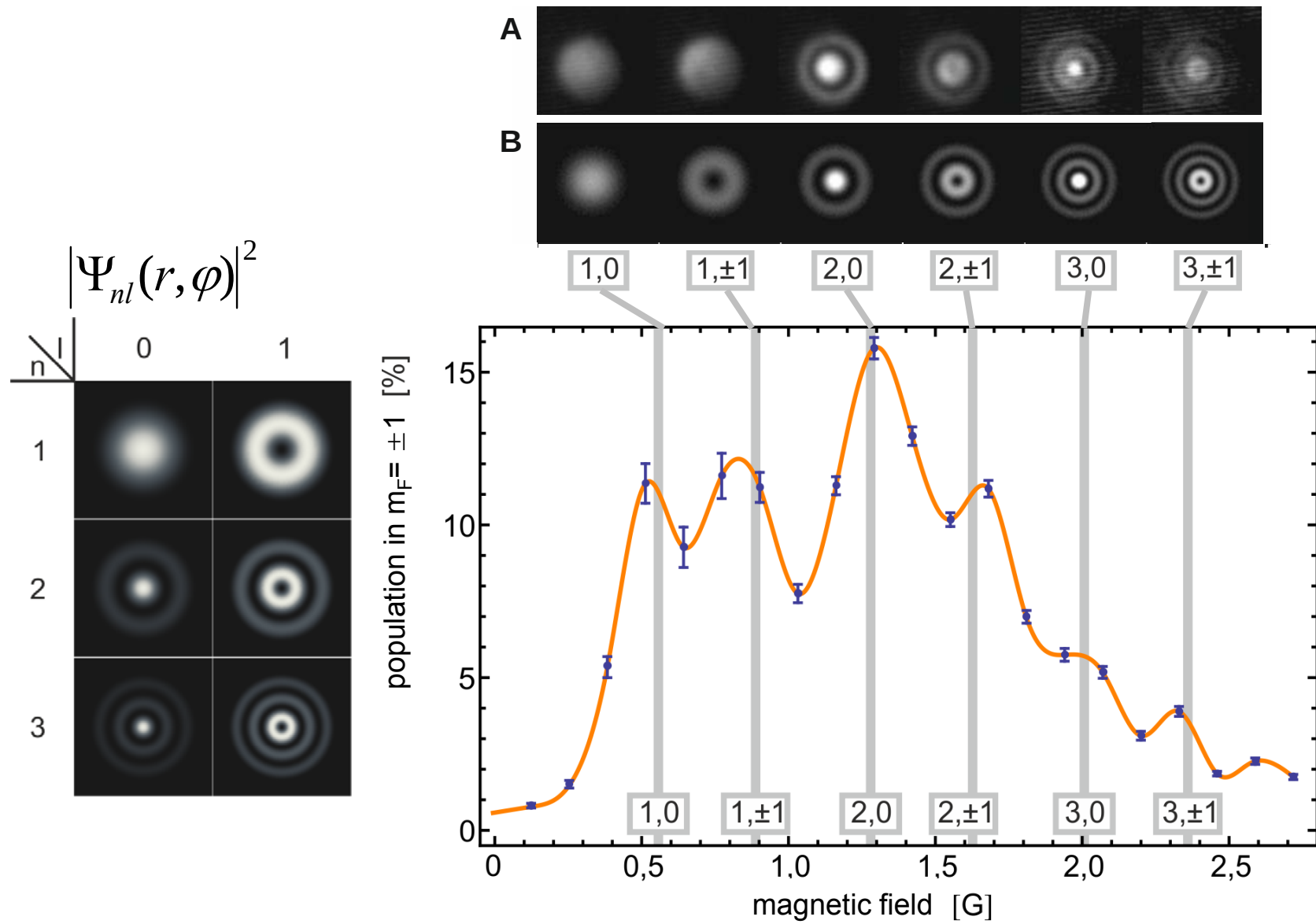
Effective potential for $m_F = \pm 1$ atoms



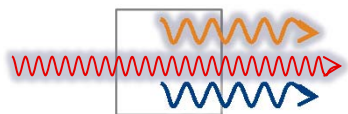
Simplified model for spin dynamics

Effective potential for $m_F = \pm 1$ atoms





Content



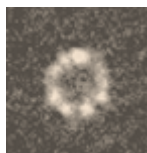
Introduction



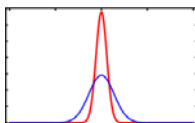
Creation of correlated states



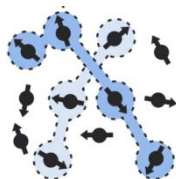
External mode control



2D correlated spinor gasses

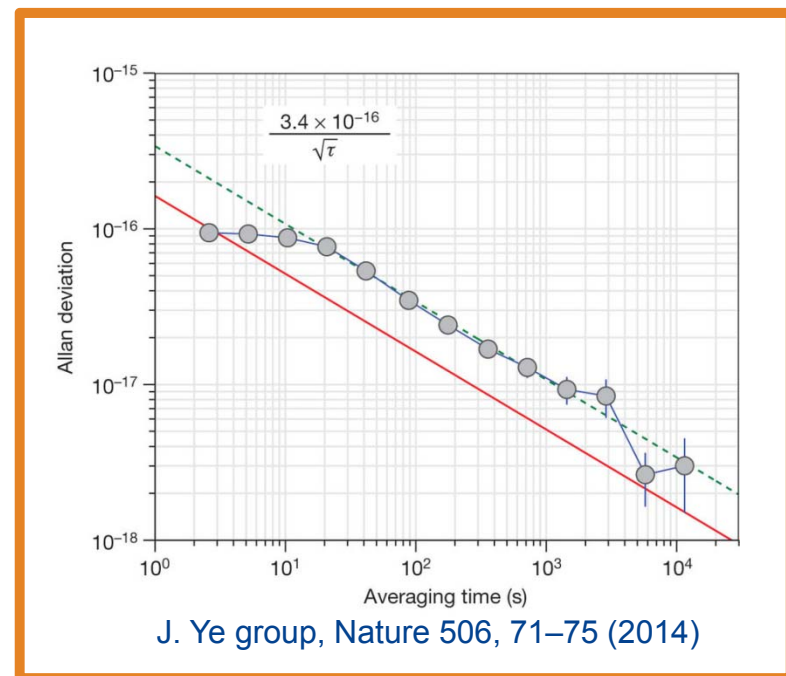
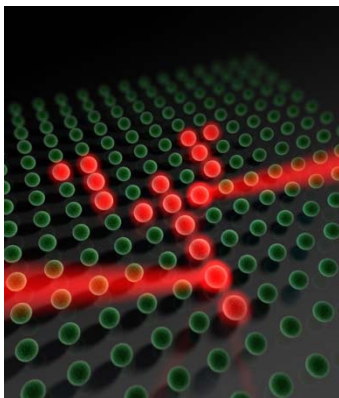
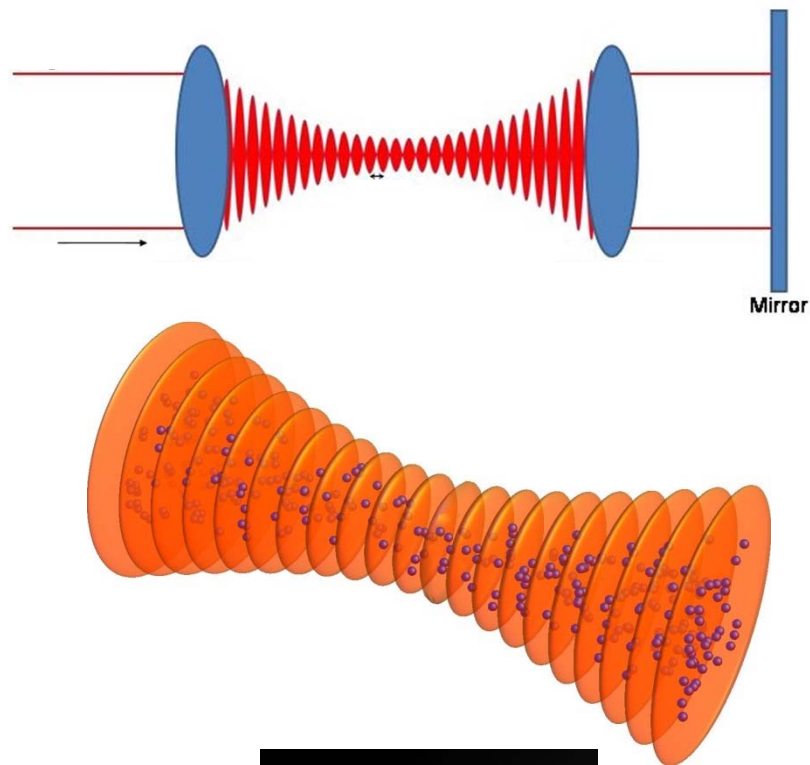


Squeezed and Dicke states

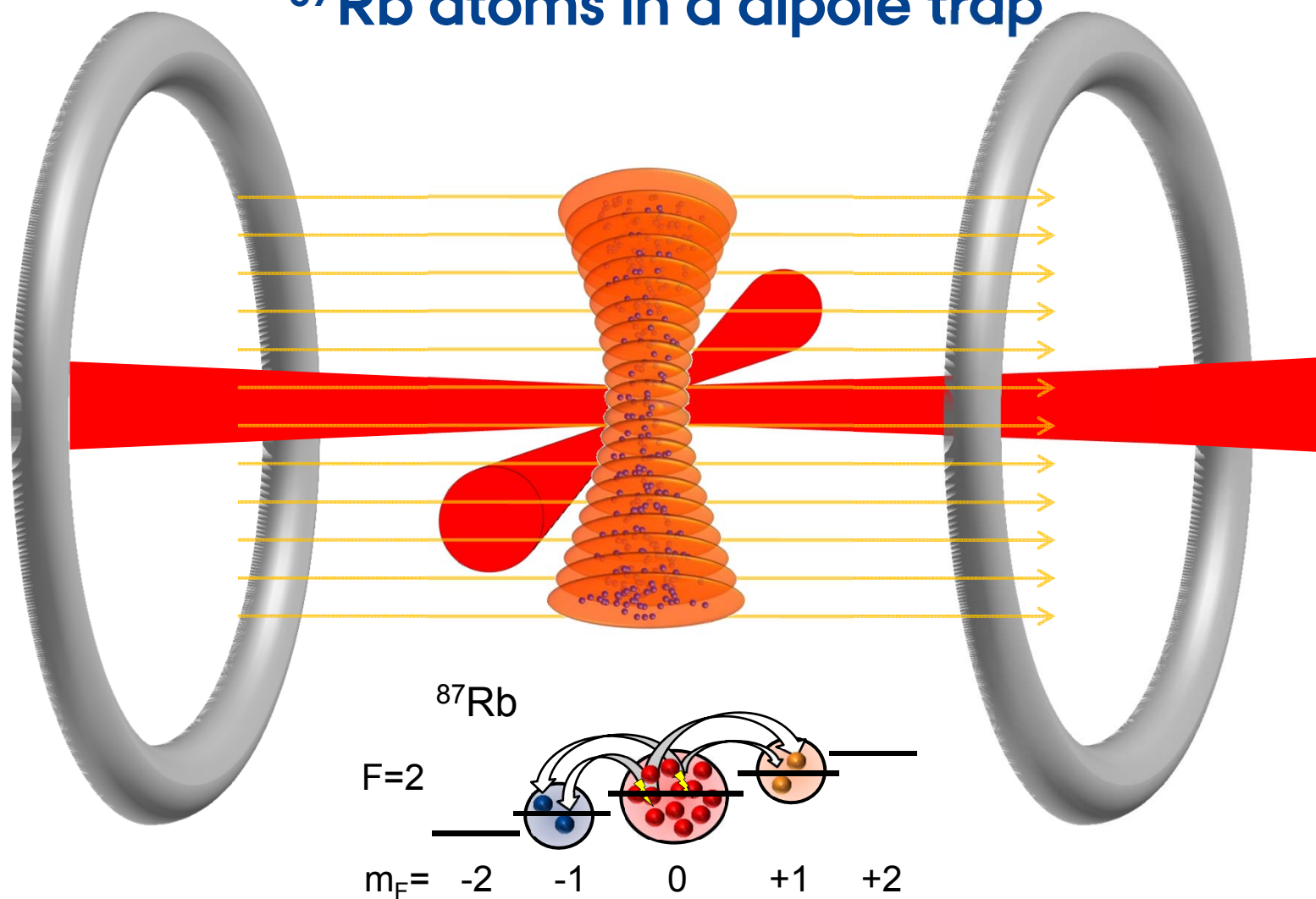


Multi-particle entanglement

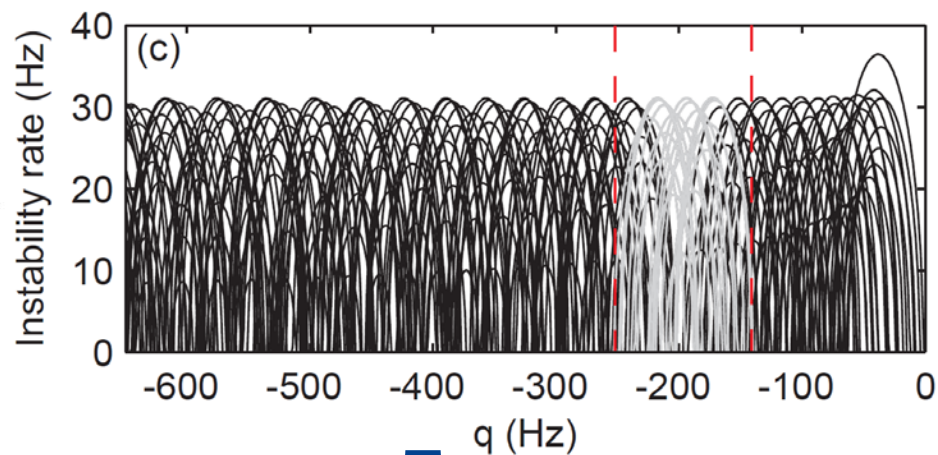
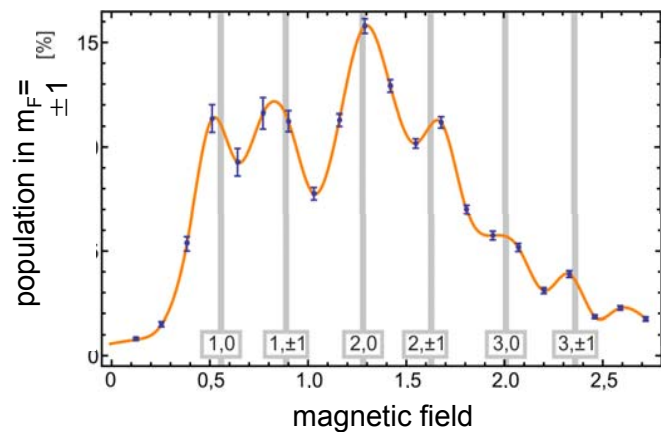
Optical lattices



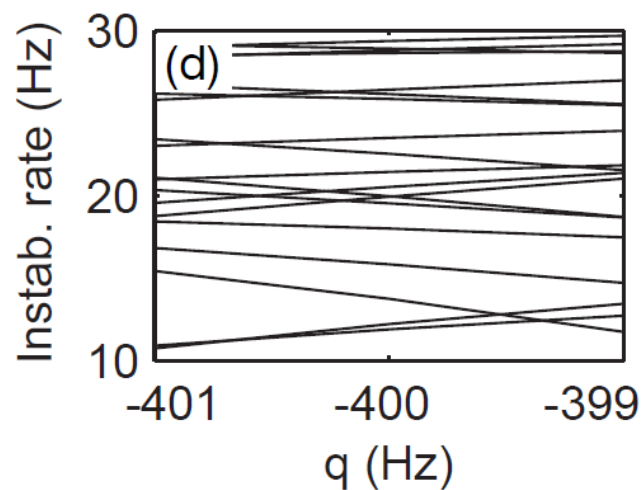
^{87}Rb atoms in a dipole trap



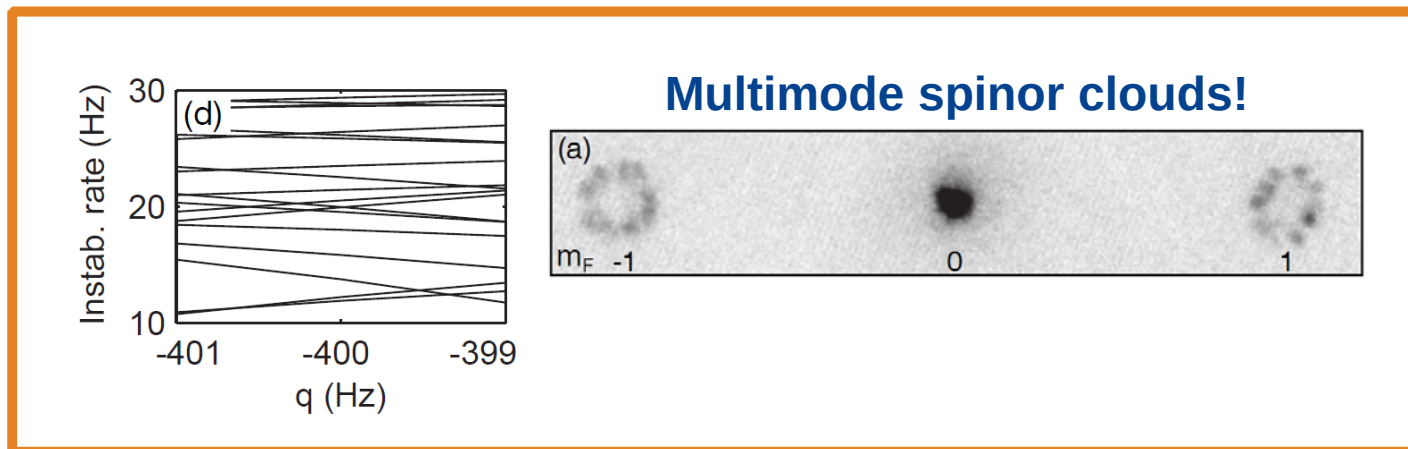
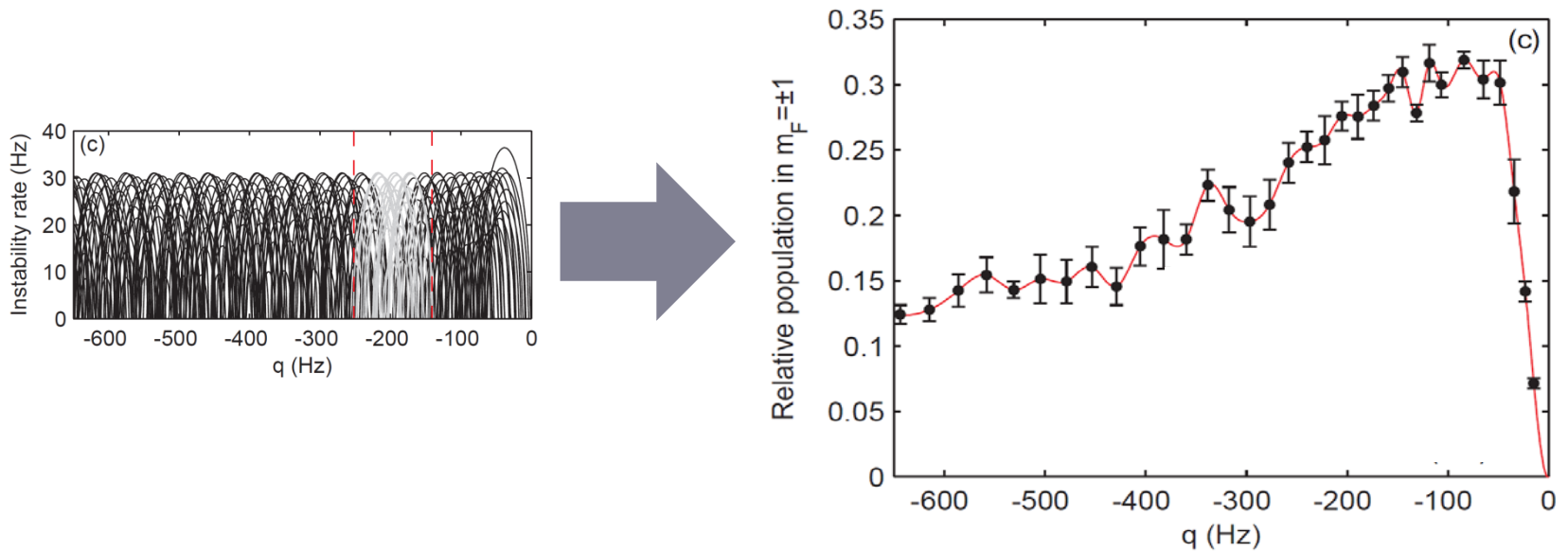
External modes in 2D



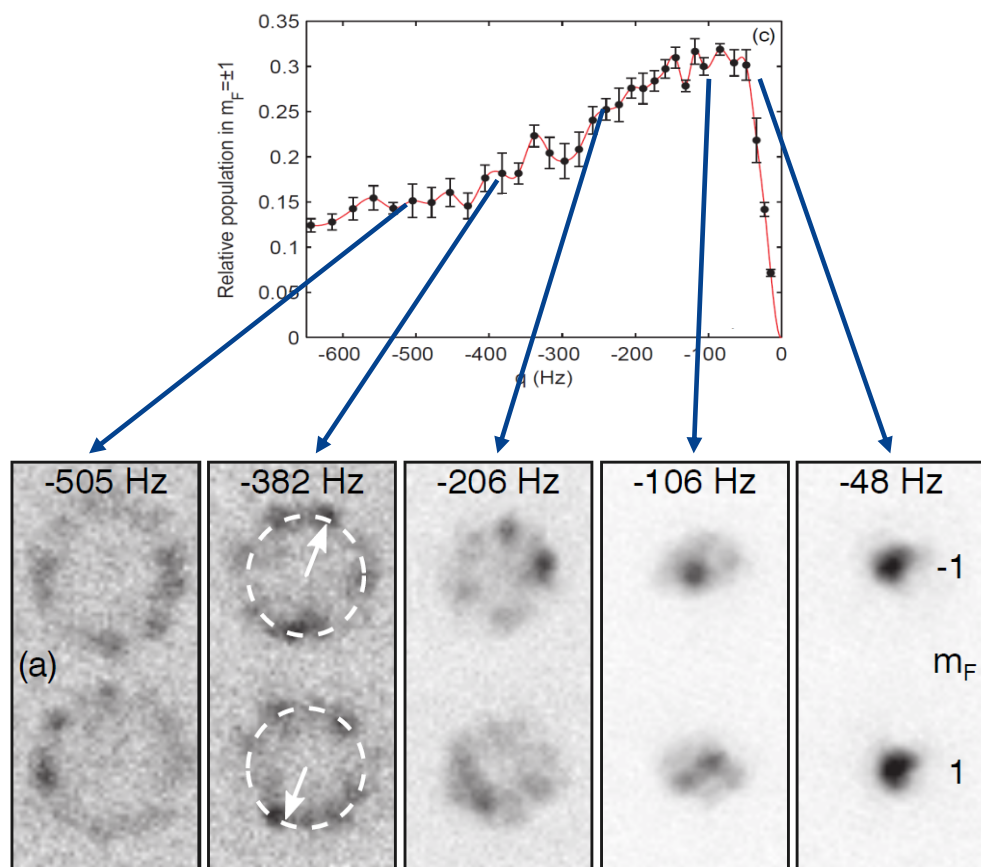
**Multimode dynamics
expected!**



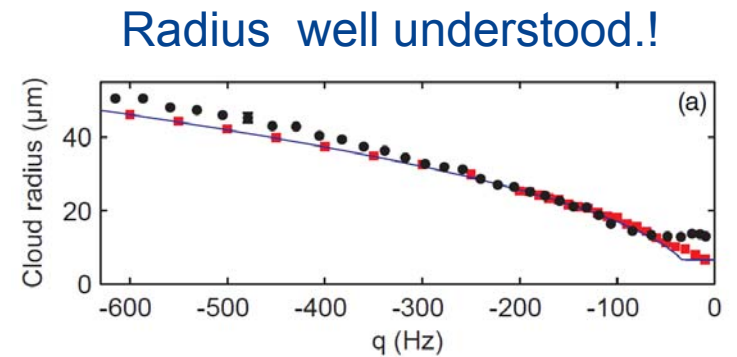
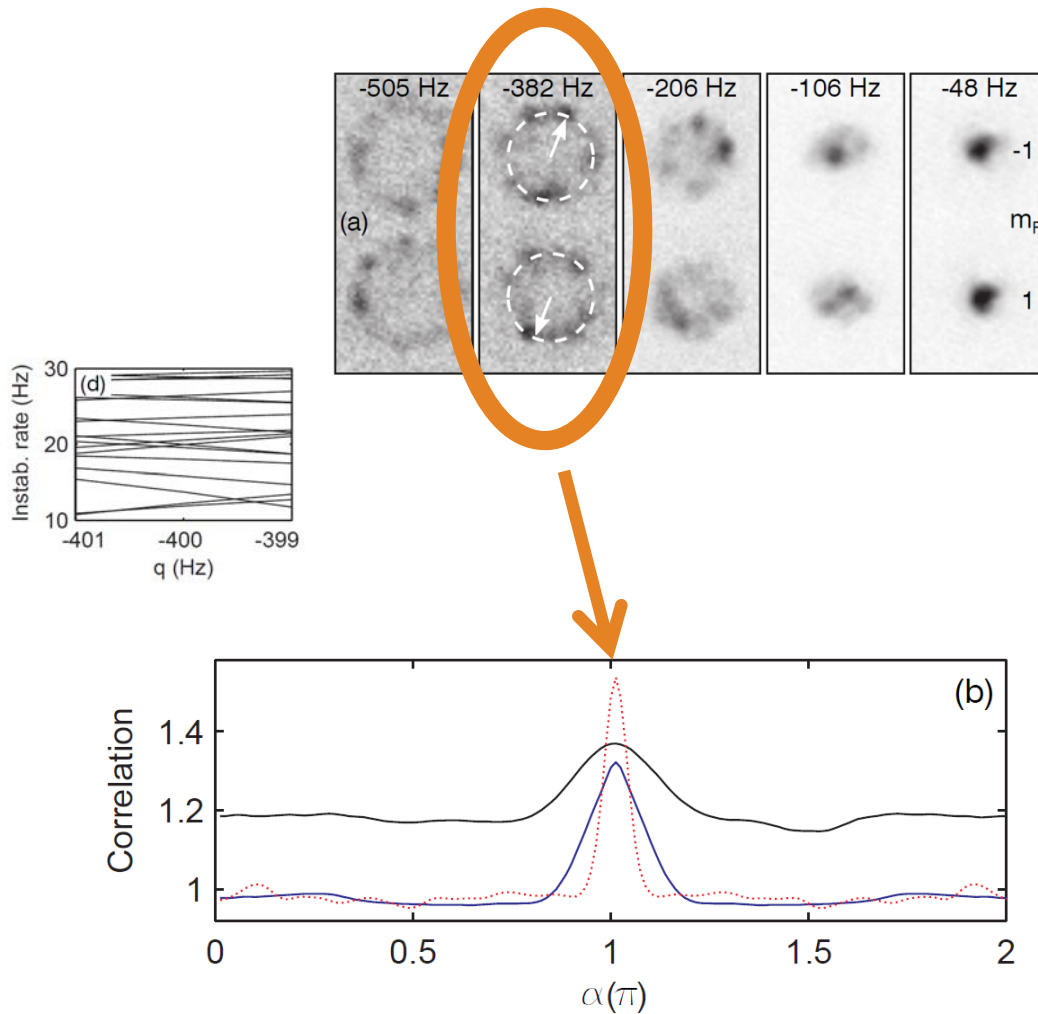
External modes in 2D



Observation of “correlated rings” in TOF

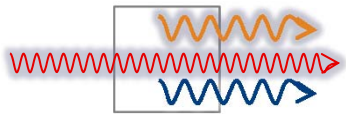


Understanding “correlated rings” in TOF



- Correlated clouds
- Squeezed relative atom number
- EPR pairs?

Content



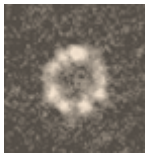
Introduction



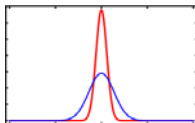
Creation of correlated states



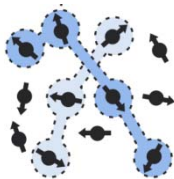
External mode control



2D correlated spinor gasses



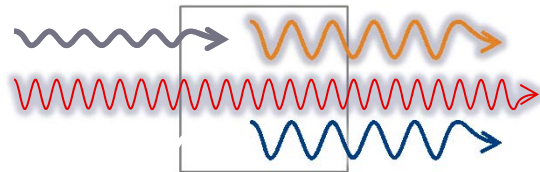
Dicke states for interferometry



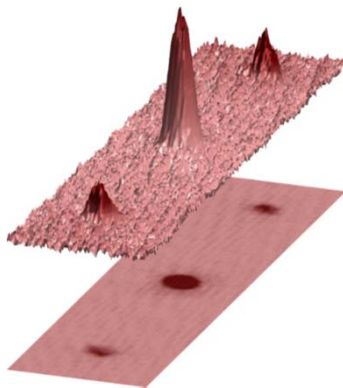
Multi-particle entanglement

Two possibilities for triggering:

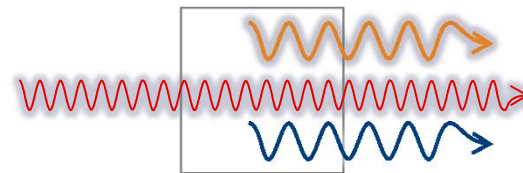
1) classical seed



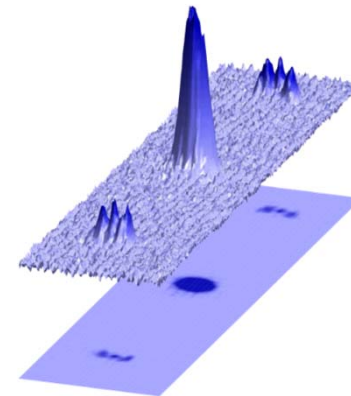
Seed atoms in $m_F = \pm 1$ in the spatial mode of the initial BEC



2) vacuum fluctuations



No atoms present in $m_F = \pm 1$ in the excited spatial mode

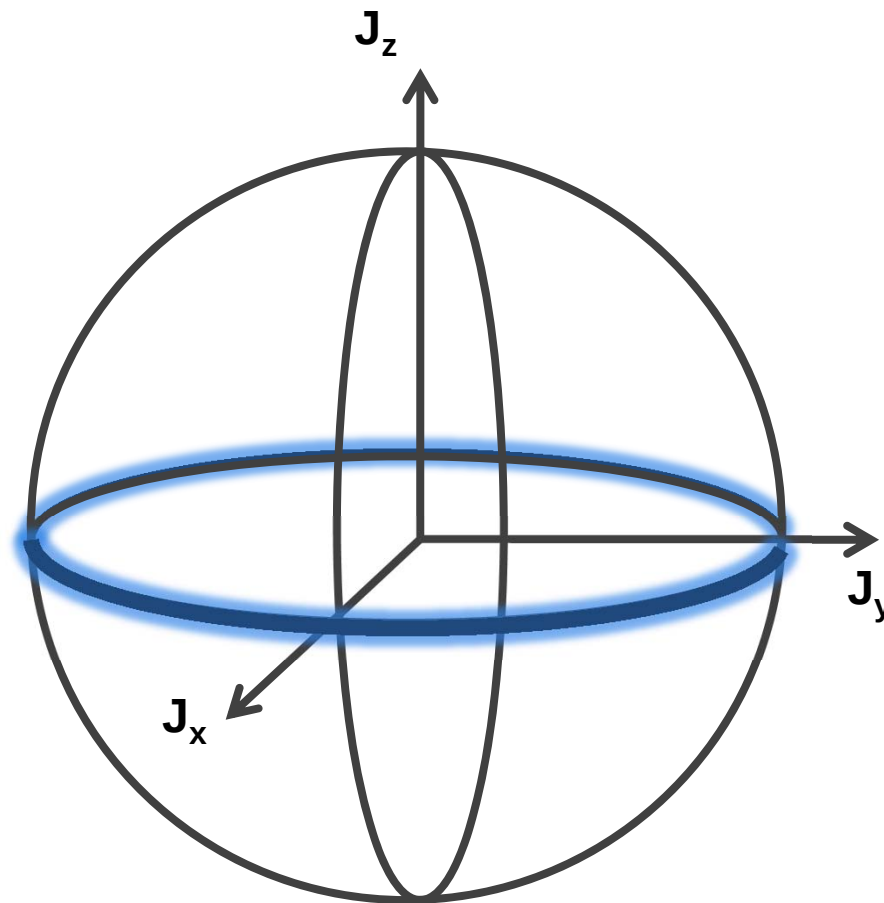


Dicke states

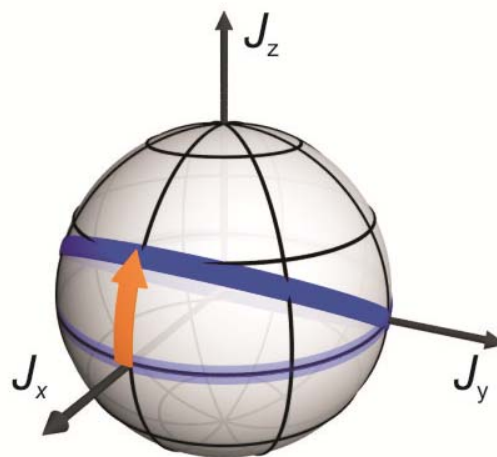
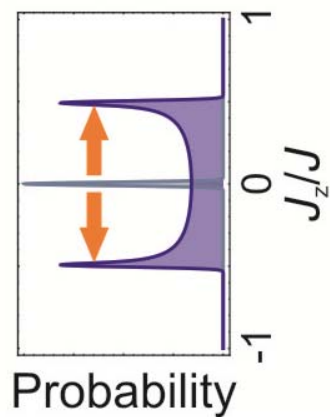
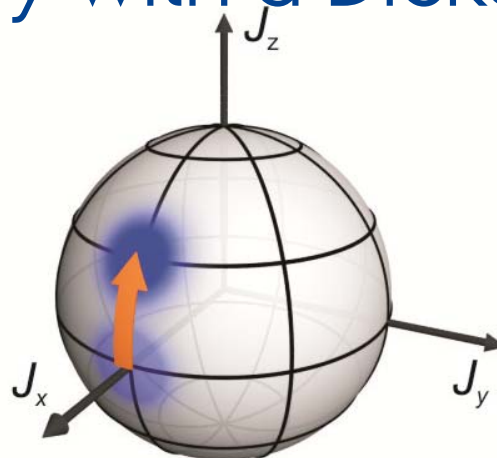
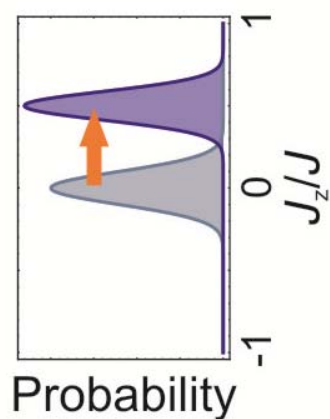
Ideally, spin dynamics produces a Dicke state with the following properties:

$$\Delta J_z = 0$$

$$\langle J_x \rangle = \langle J_y \rangle = 0$$

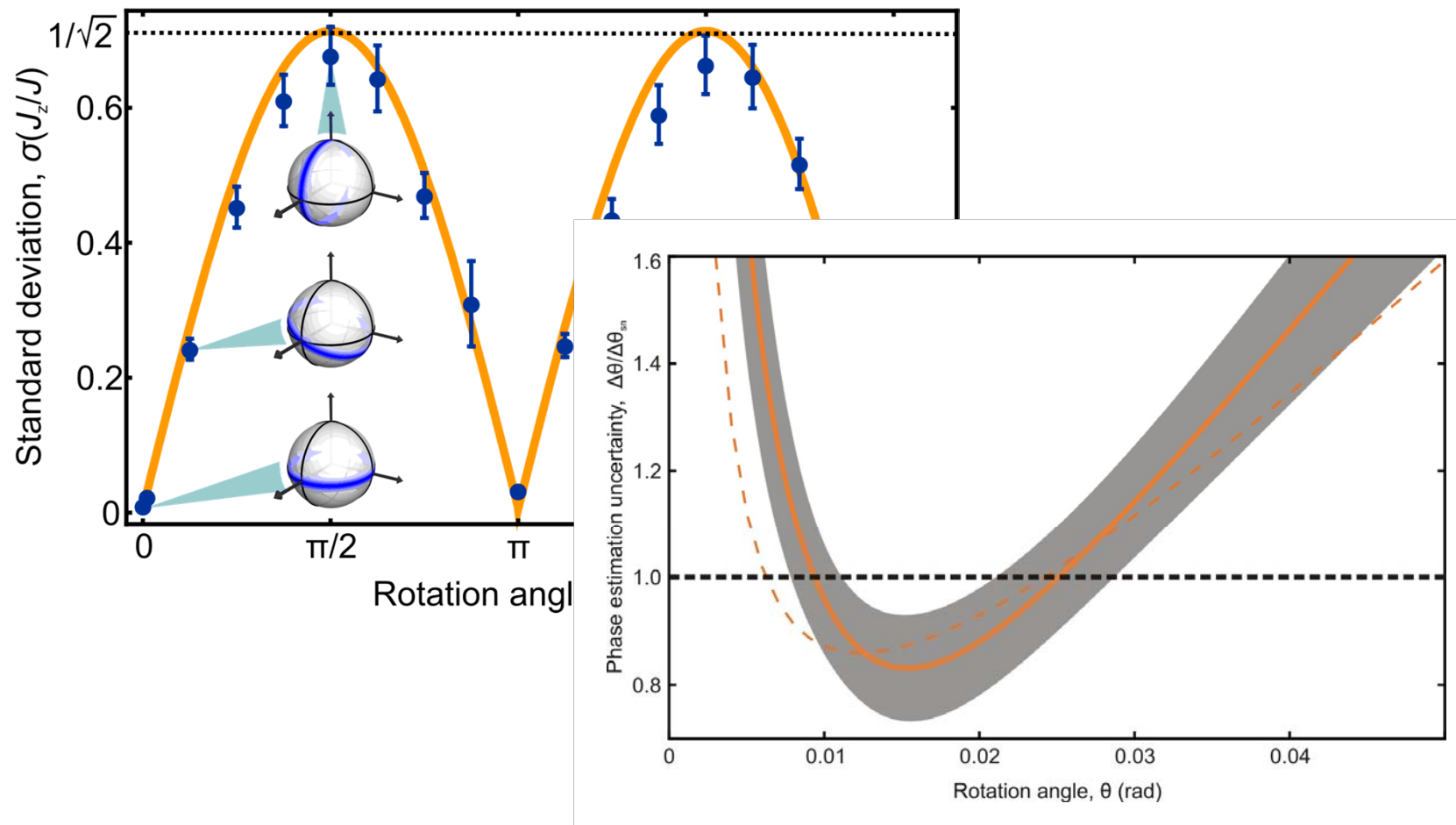


Interferometry with a Dicke state

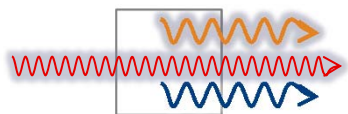


Observable: $\sigma(J_z)$

Standard deviation after rotation



Content



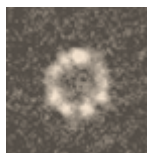
Introduction



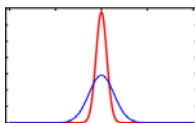
Creation of correlated states



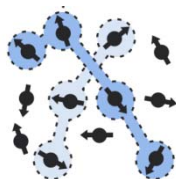
External mode control



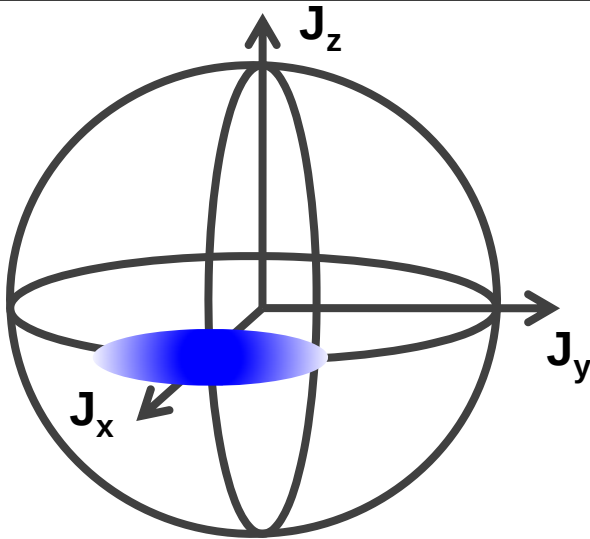
2D correlated spinor gasses



Dicke states for interferometry



Multi-particle entanglement

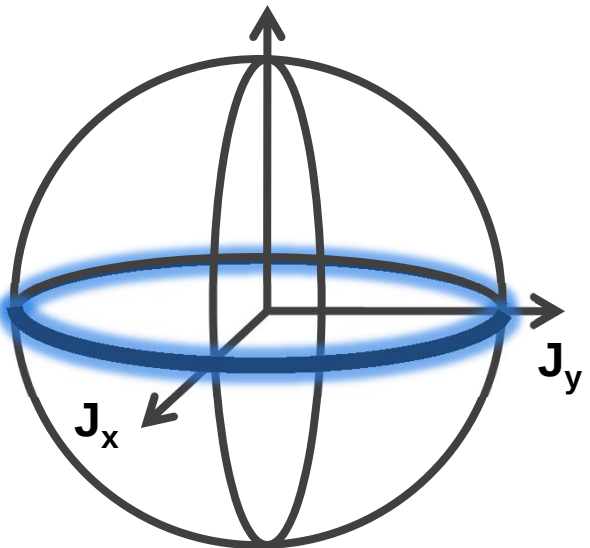


Spin squeezing parameter

$$\xi^2 = N \frac{(\Delta J_z)^2}{\langle J_x \rangle^2 + \langle J_y \rangle^2}$$

$\xi < 1$ proves entanglement

D.J.Wineland, J.J.Bollinger and W.M.Itano, *Squeezed atomic states and projection noise in spectroscopy*, Phys. Rev. A 50, 67–88 (1994)



Generalized squeezing parameter

$$\xi_{\text{gen}}^2 = (N - 1) \frac{(\Delta J_z)^2}{\langle J_x^2 \rangle + \langle J_y^2 \rangle - N/2}$$

$\xi < 1$ proves entanglement

G. Vitaliano, P. M. F. de Oliveira, J. G. M. de Oliveira, *Entanglement in arbitrary spin F*

G. Vitaliano, I. *entanglement*

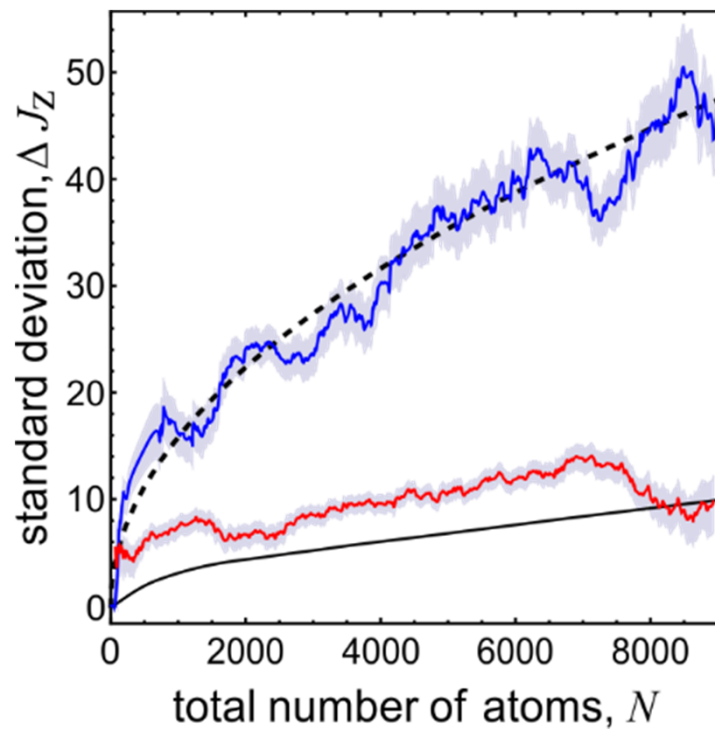
Effective spin length J_{eff}

Fluctuations in J_z



Generalized squeezing parameter

$$\xi_{\text{gen}}^2 = (N - 1) \frac{(\Delta J_z)^2}{\langle J_x^2 \rangle + \langle J_y^2 \rangle - N/2}$$

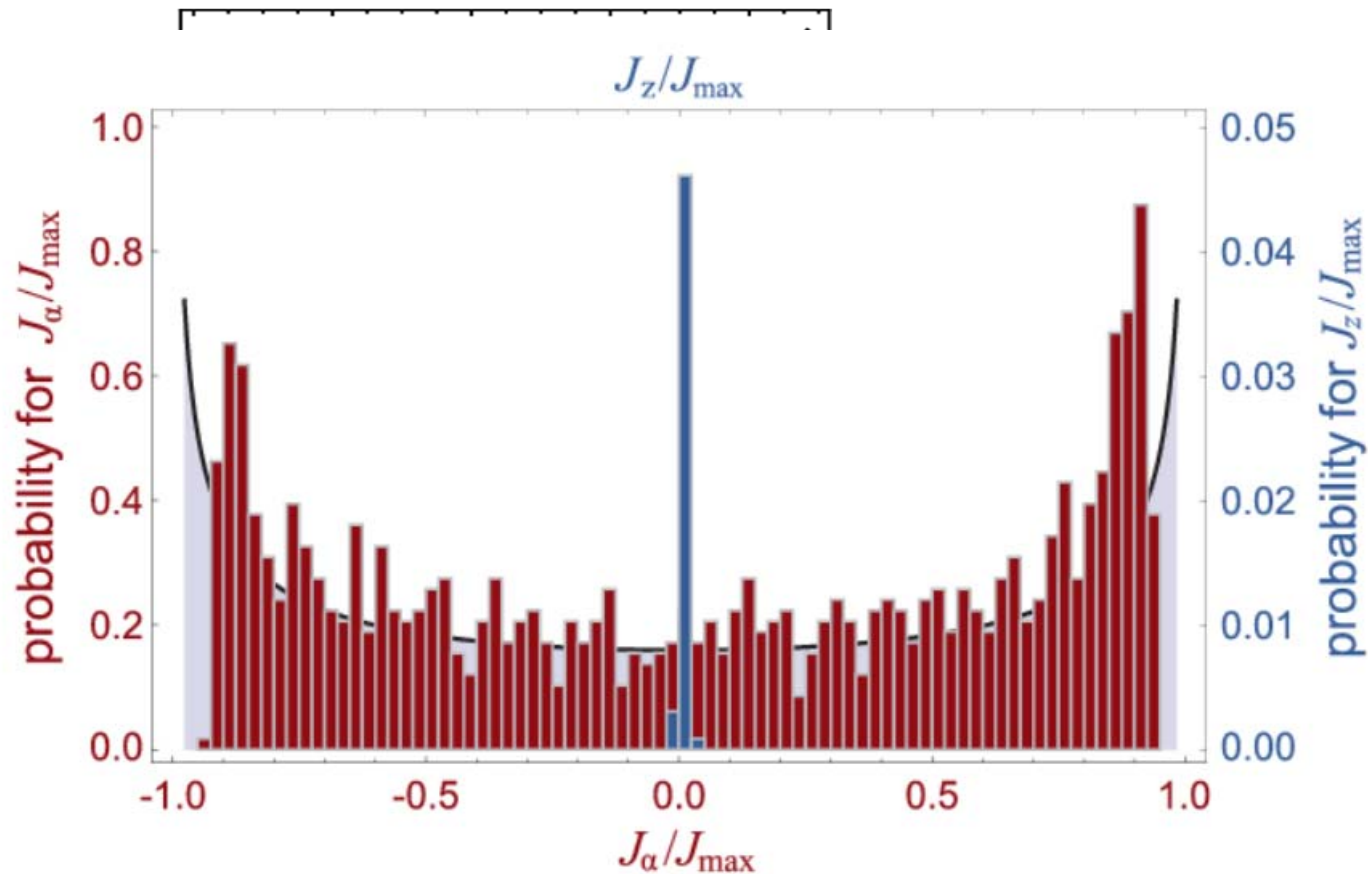


number squeezing:
-12.4 ± 1.2 dB

Fluctuations in J_{eff}

Generalized squeezing parameter

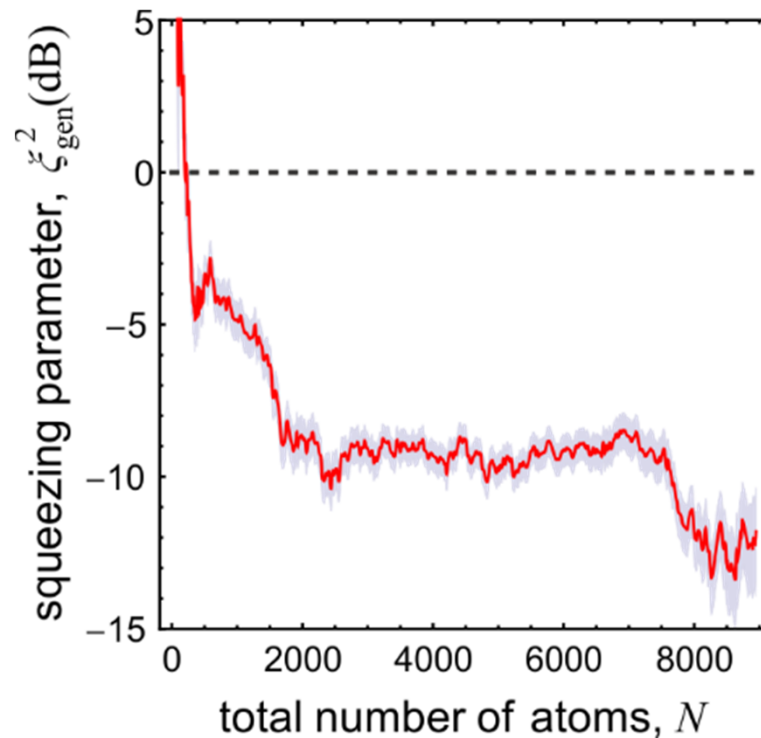
$$\xi_{\text{gen}}^2 = (N - 1) \frac{(\Delta J_z)^2}{\langle J_x^2 \rangle + \langle J_y^2 \rangle - N/2}$$



Generalized spin squeezing

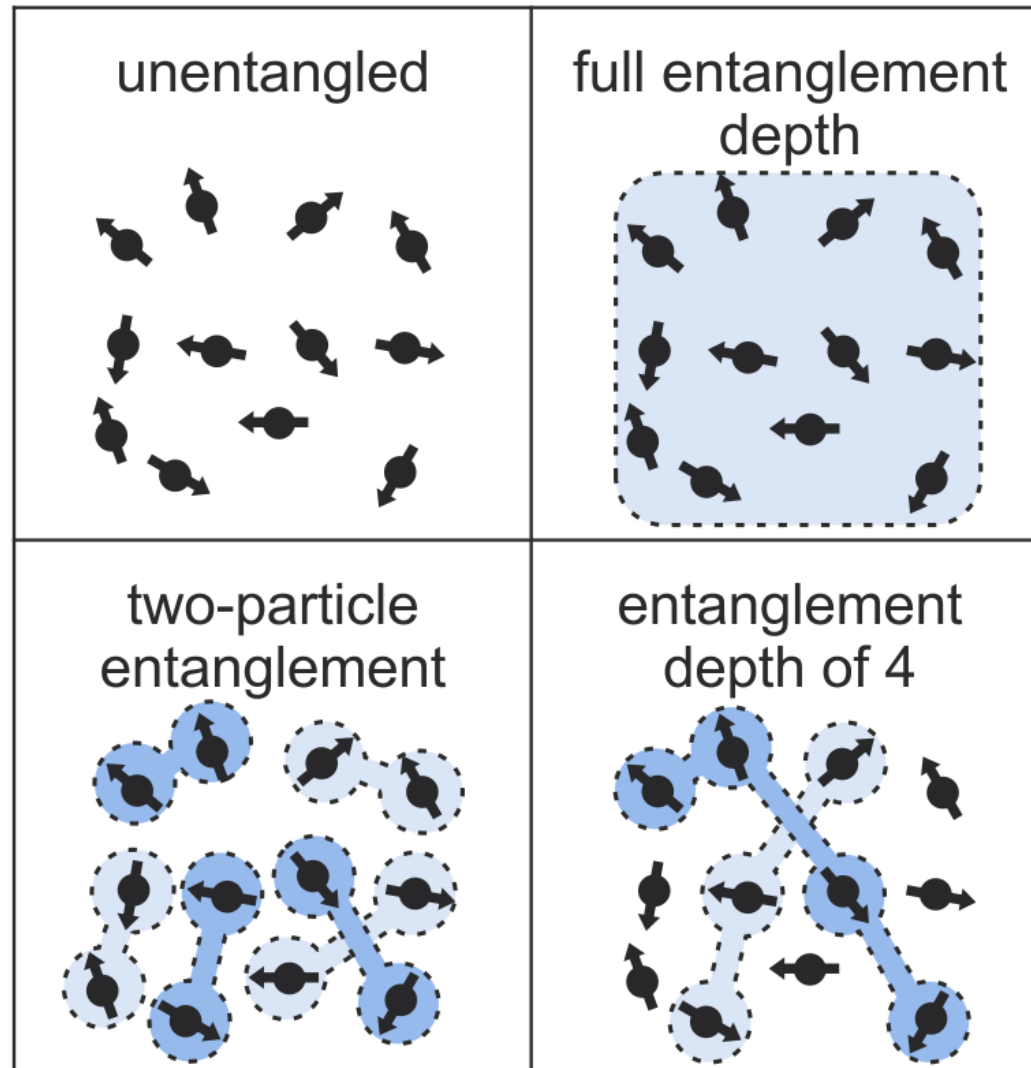
Generalized squeezing parameter

$$\xi_{\text{gen}}^2 = (N - 1) \frac{(\Delta J_z)^2}{\langle J_x^2 \rangle + \langle J_y^2 \rangle - N/2}$$

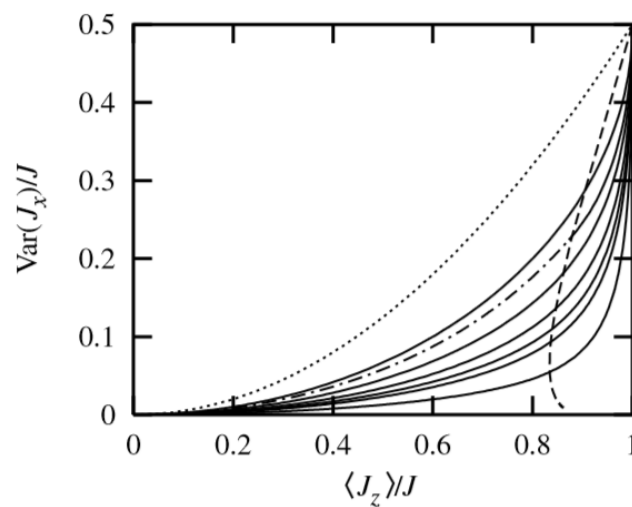
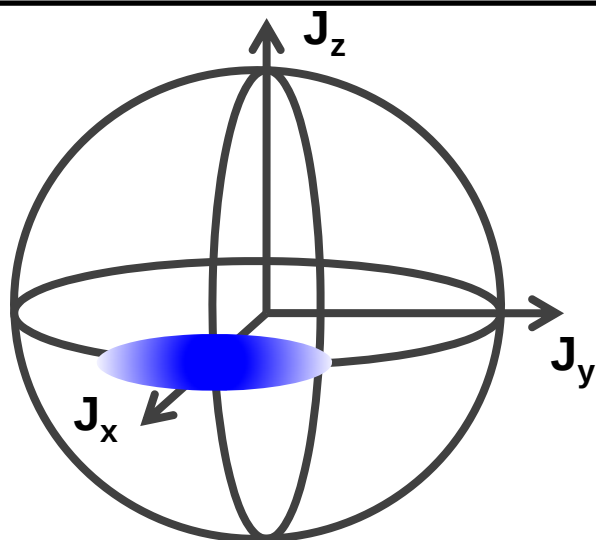


generalized squeezing:
-11.4(5) dB at 8000 atoms

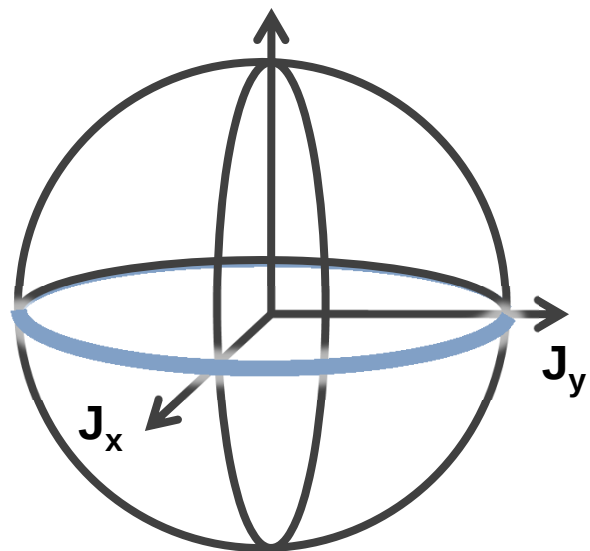
Entanglement depth



Entanglement depth



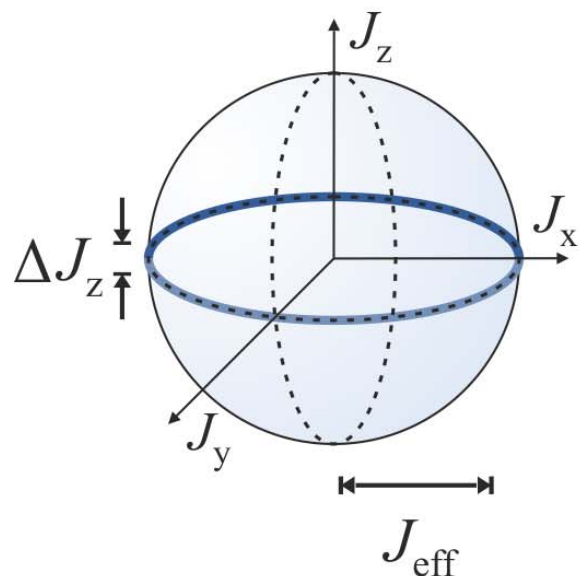
A. Sørensen and
B. K. Mølmer,
Phys. Rev. Lett.
86, 4431 (2001).



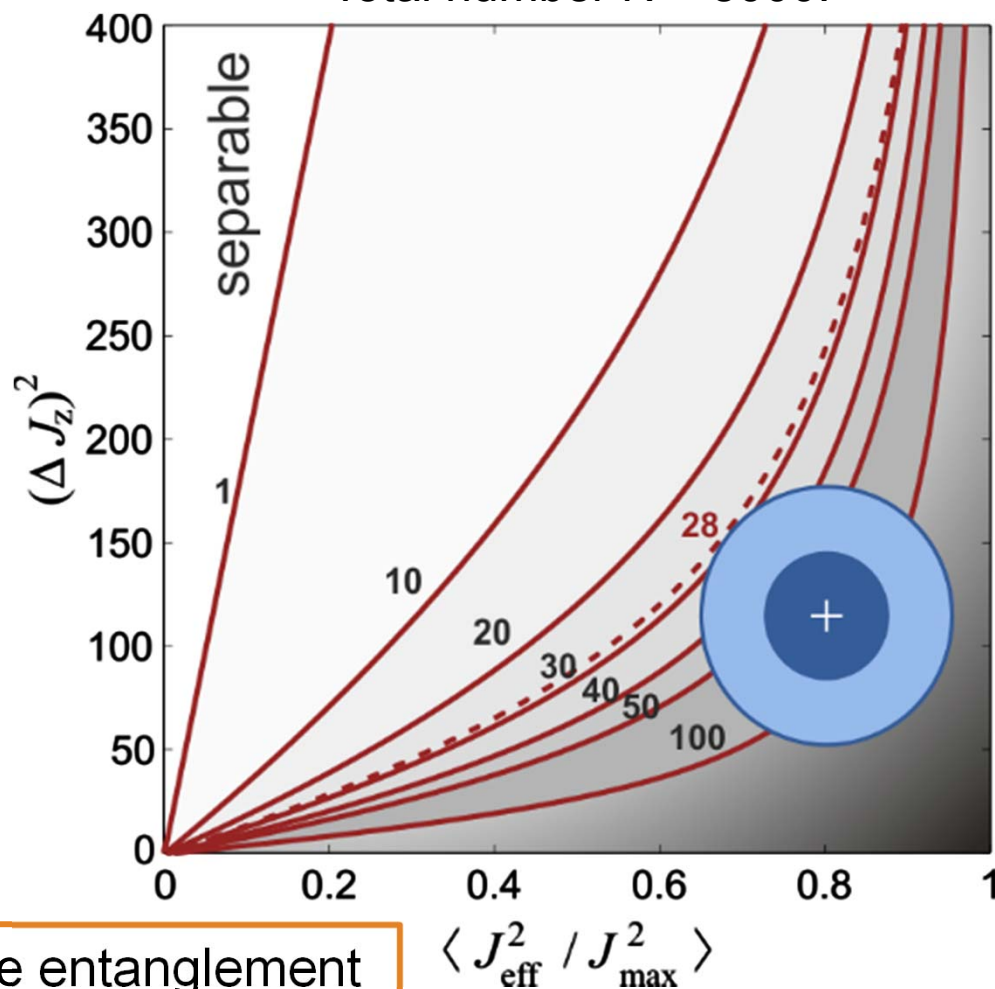
?

Measurement of the entanglement depth

Total number $N = 8000$.



$$J_{\text{eff}}^2 = \langle J_x^2 + J_y^2 \rangle$$



Center: **68-particle entanglement**
Two std. dev.: **28-particle entanglement**

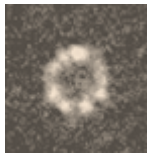
Conclusion



Creation of correlated states

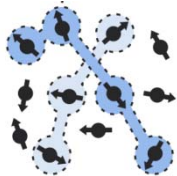


External mode control



2D correlated spinor gasses

- observation in single planes
- EPR state preparation



Multi-particle entanglement

- interferometry with heralded Fock states
- deterministic preparation of Dicke states

Thank you for your attention.

P. Pedersen, M. Gajdacz, J. Sherson, A. Hilliard

Aarhus Universitet



B. Lücke, J. Peise, F. Deuretzbacher,
W. Ertmer, L. Santos, C. Klempt

Leibniz Universität Hannover

G. Vitagliano, G. Tóth

University of the Basque Country

